

# A brief introduction to Computational Neuroscience

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Sophie Deneve

Group for Neural Theory  
Ecole normale supérieure Paris



# Computational Neuroscience Introduction Day

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- 14.00 Introduction
- 14.30 Computational Neuroscience Groups in Paris
- 15.00 Discussion of papers in groups: Questions
- 15.45 Break
- 16.00 Discussion of papers in groups: Answers
- 16.45 Presentation of Answers
- 17.30 Concluding comments

# What's the brain good for?



Tree  
no neurons

# What's the brain good for?



Tree  
no neurons



C. elegans  
302 neurons

brains generate motion  
( = behavior)

# What's the brain good for?



Tree  
no neurons



C. elegans  
302 neurons



Fly  
1 000 000

more complex brains  
generate a greater  
variety of behaviors

# What's the brain good for?



Tree  
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C. elegans  
302 neurons



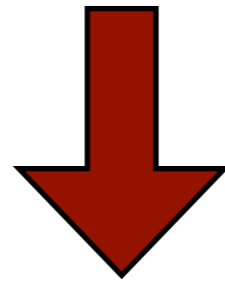
Fly  
1 000 000



Rat  
1 000 000 000



Human  
100 000 000 000



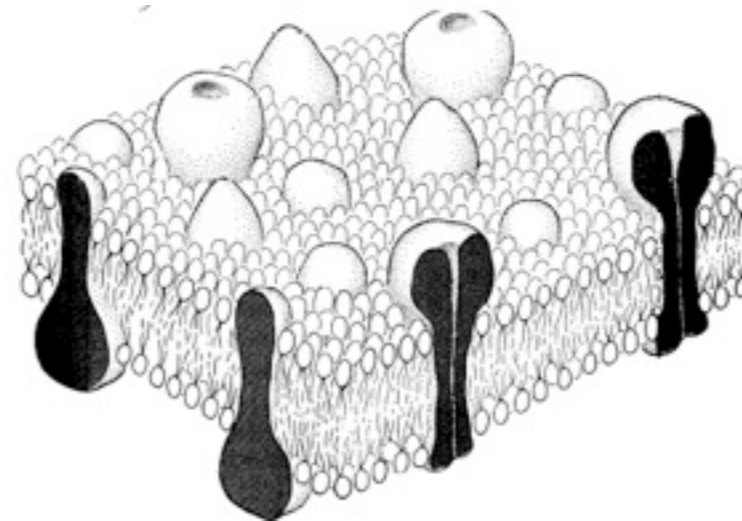
more complex brains  
generate a greater  
variety of behaviors

more complex brains  
can learn more  
behaviors

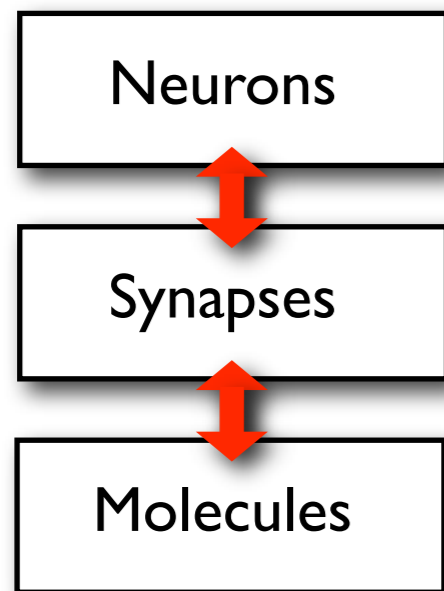
# What's the brain made of?

Molecules

1 nm



# What's the brain made of?



100  $\mu\text{m}$

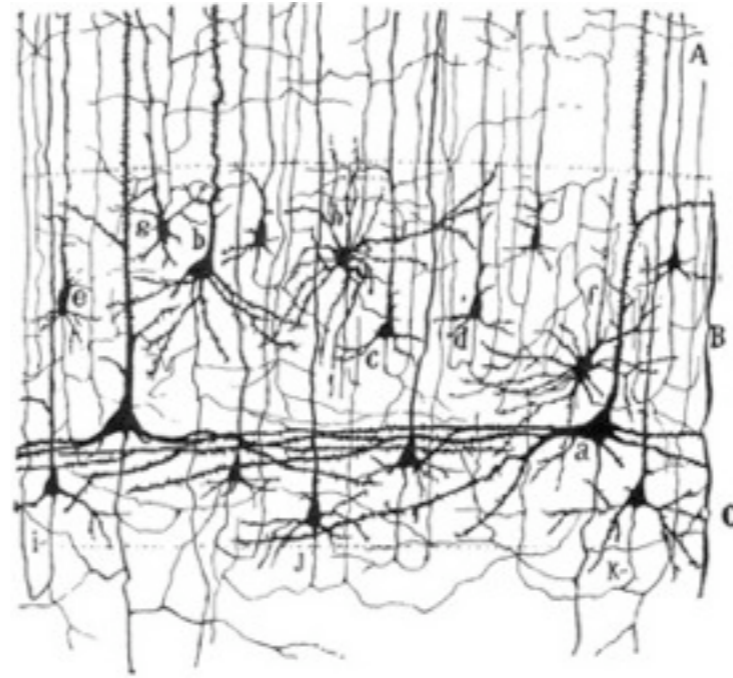
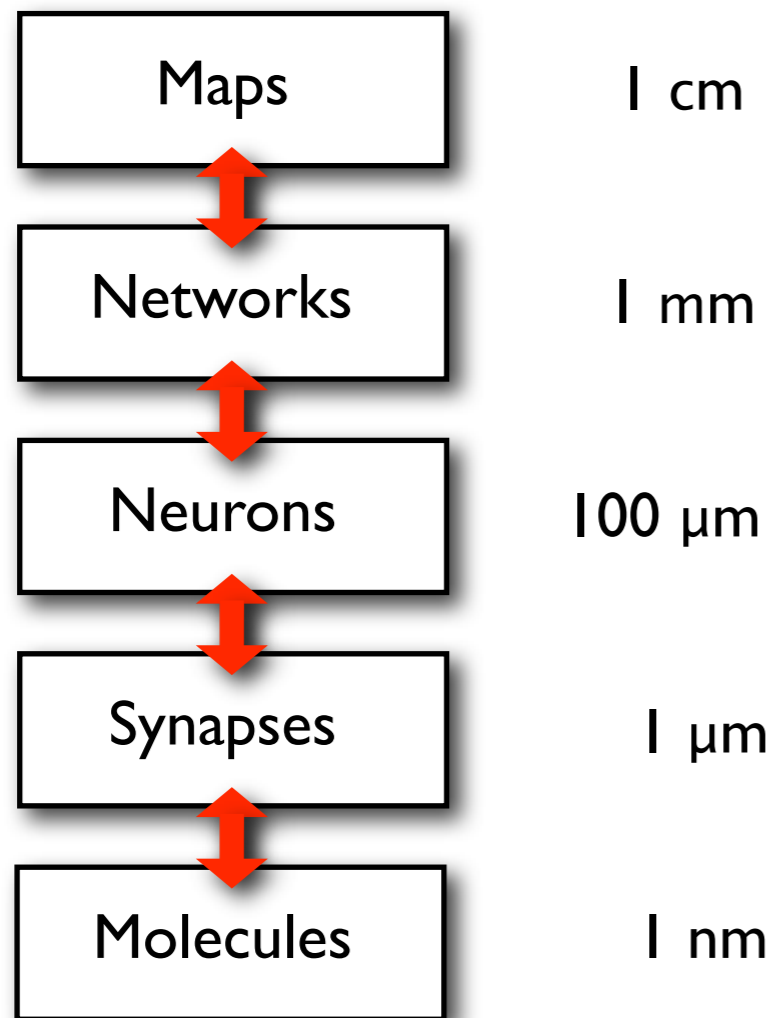
1  $\mu\text{m}$

1 nm

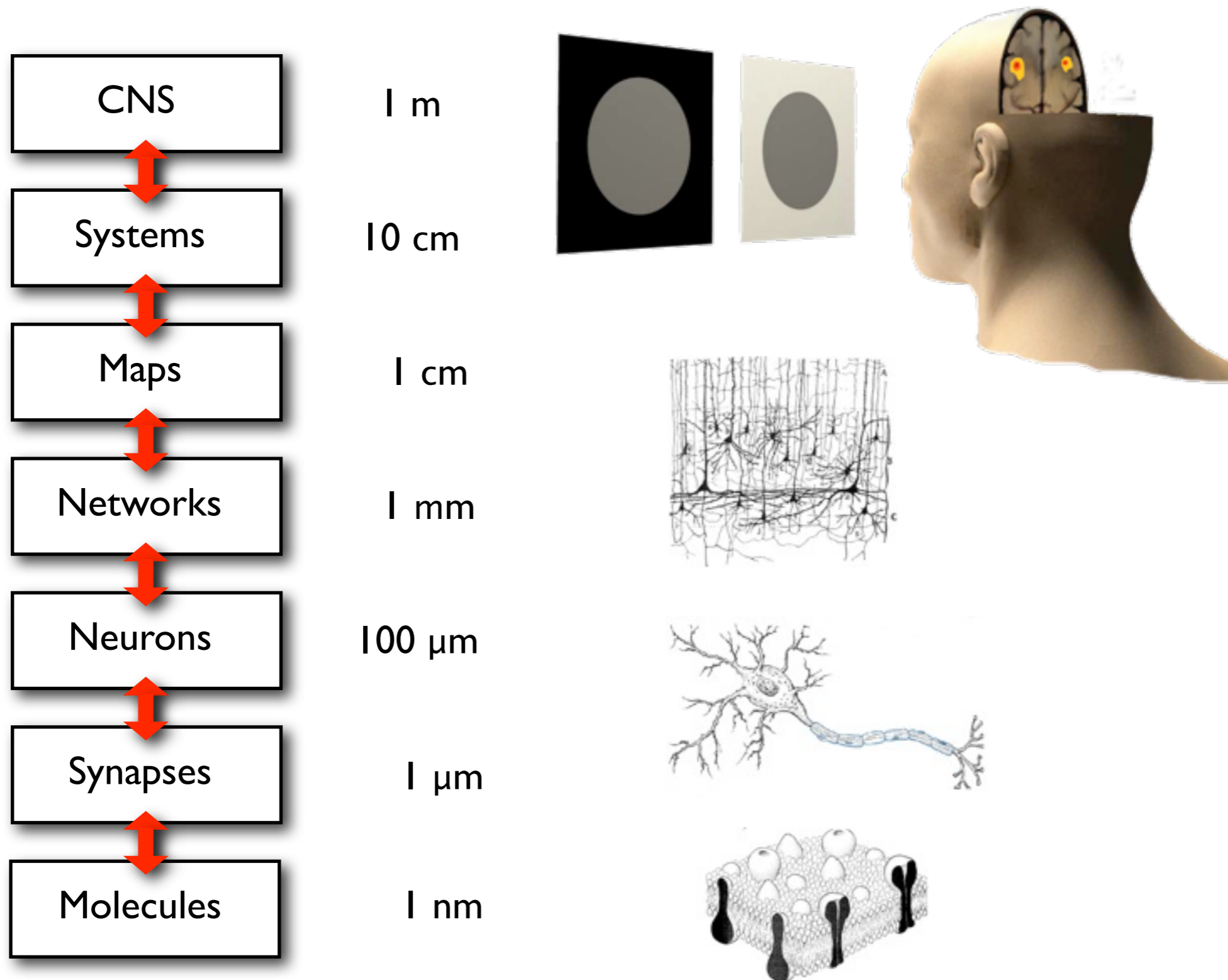




# What's the brain made of?



# What's the brain made of?



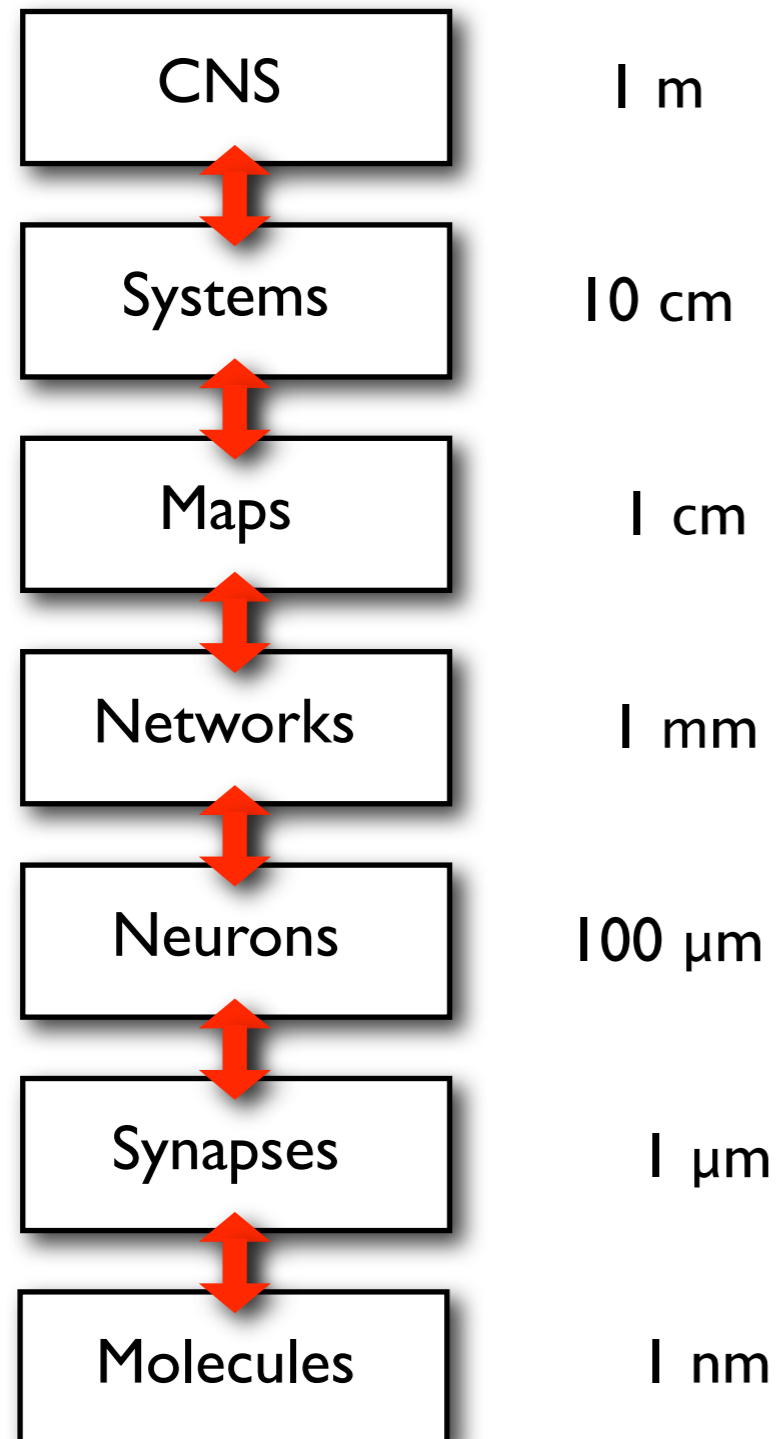
**How does the brain  
work?**

# A physics/engineering approach

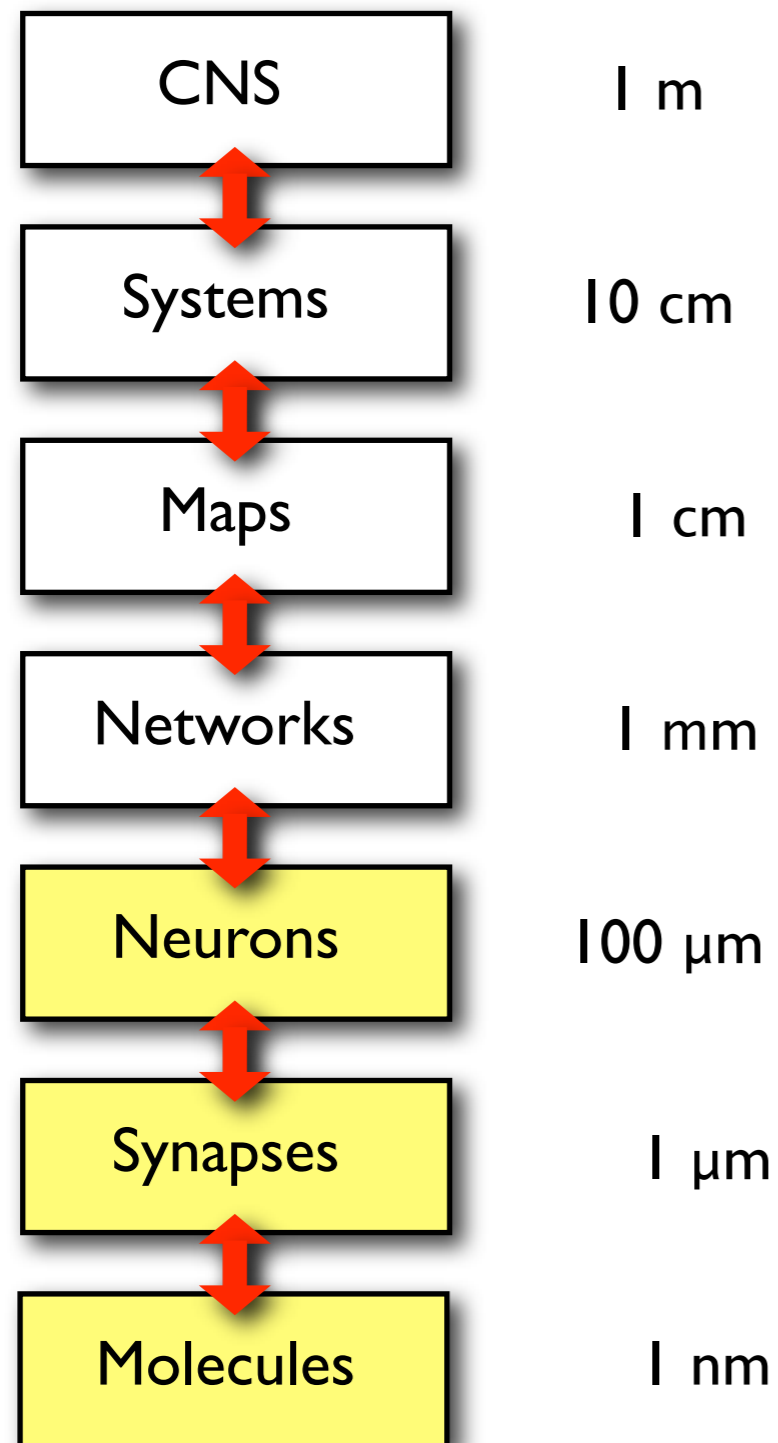
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## Just rebuild the whole thing

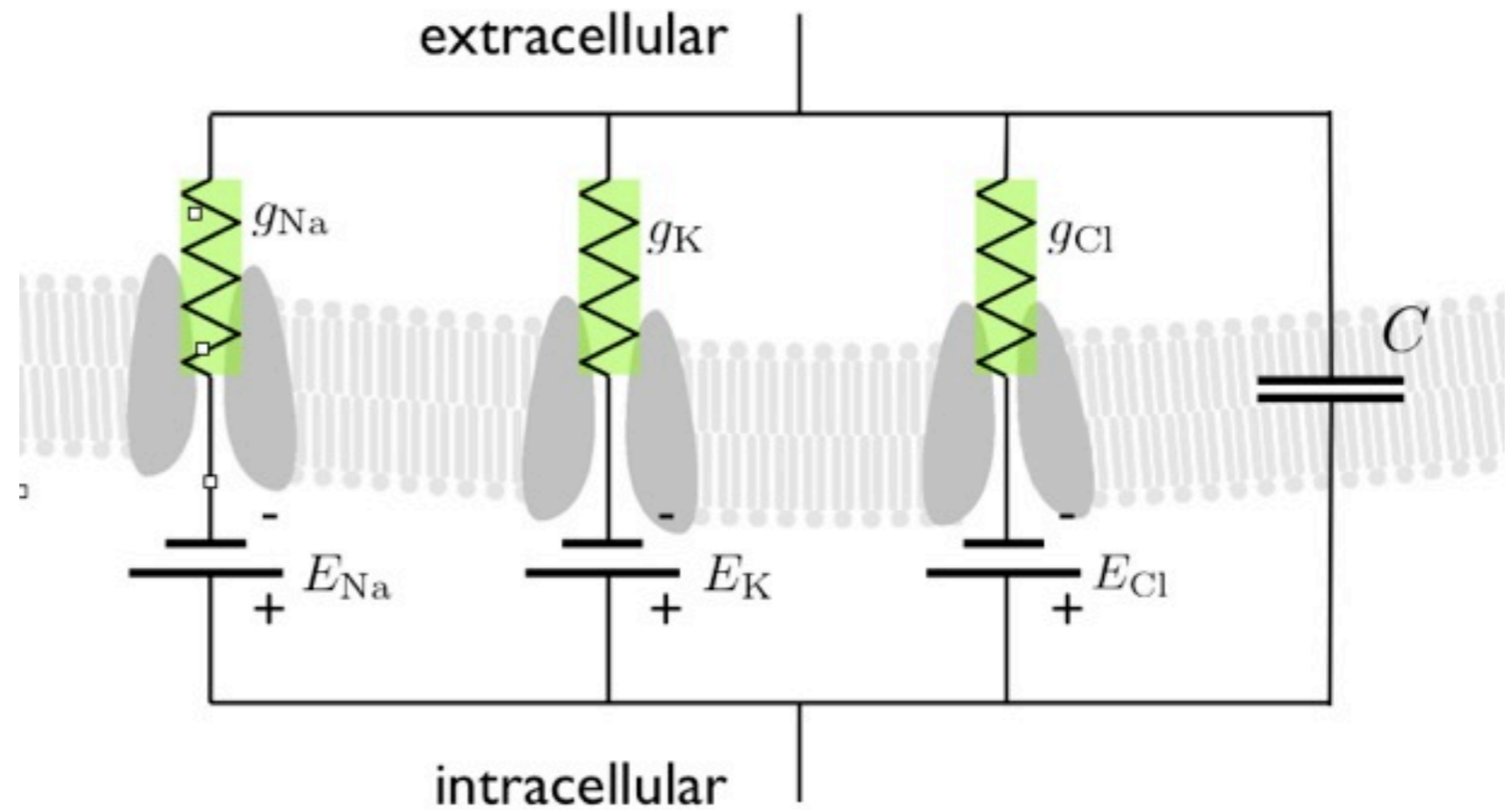
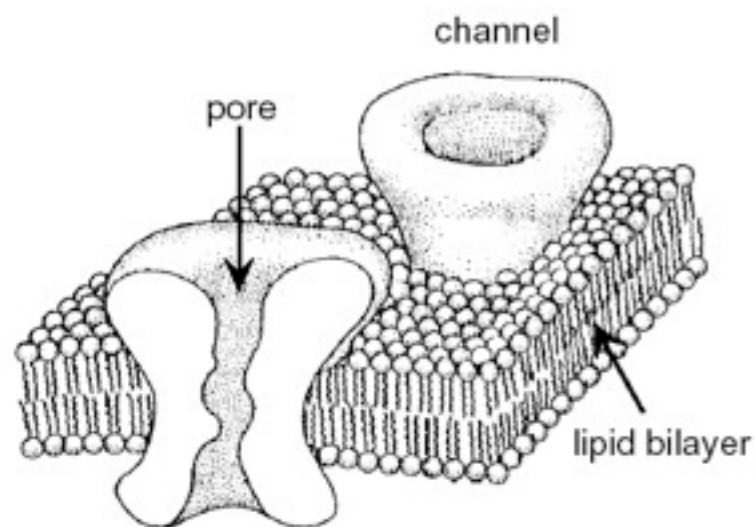
# The quest for mechanisms: Constructing systems from parts



# The quest for mechanisms: Constructing systems from parts



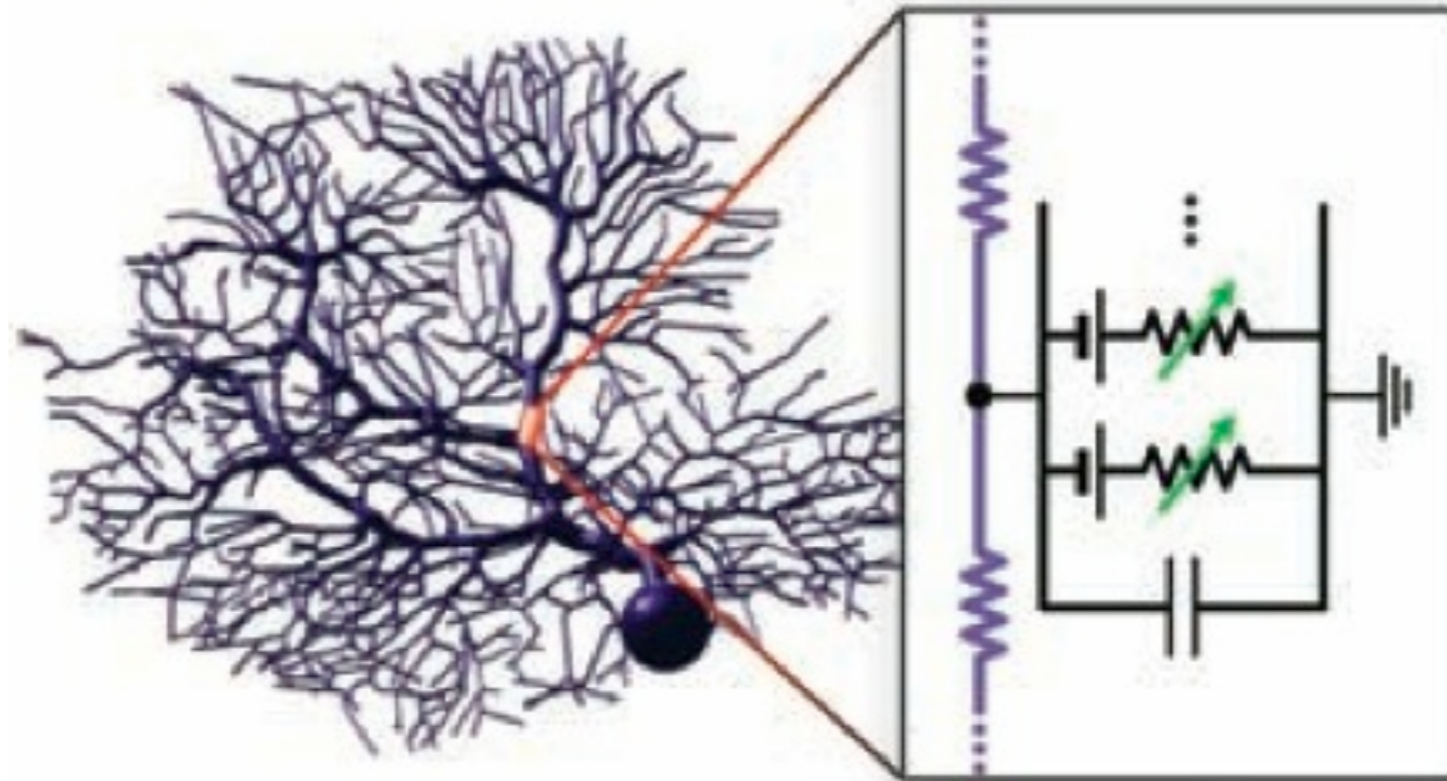
# Biophysics of the membrane voltage: The Hodgkin-Huxley Model





# Reconstructing neurons:

Ralls' cable theory and compartmental modeling

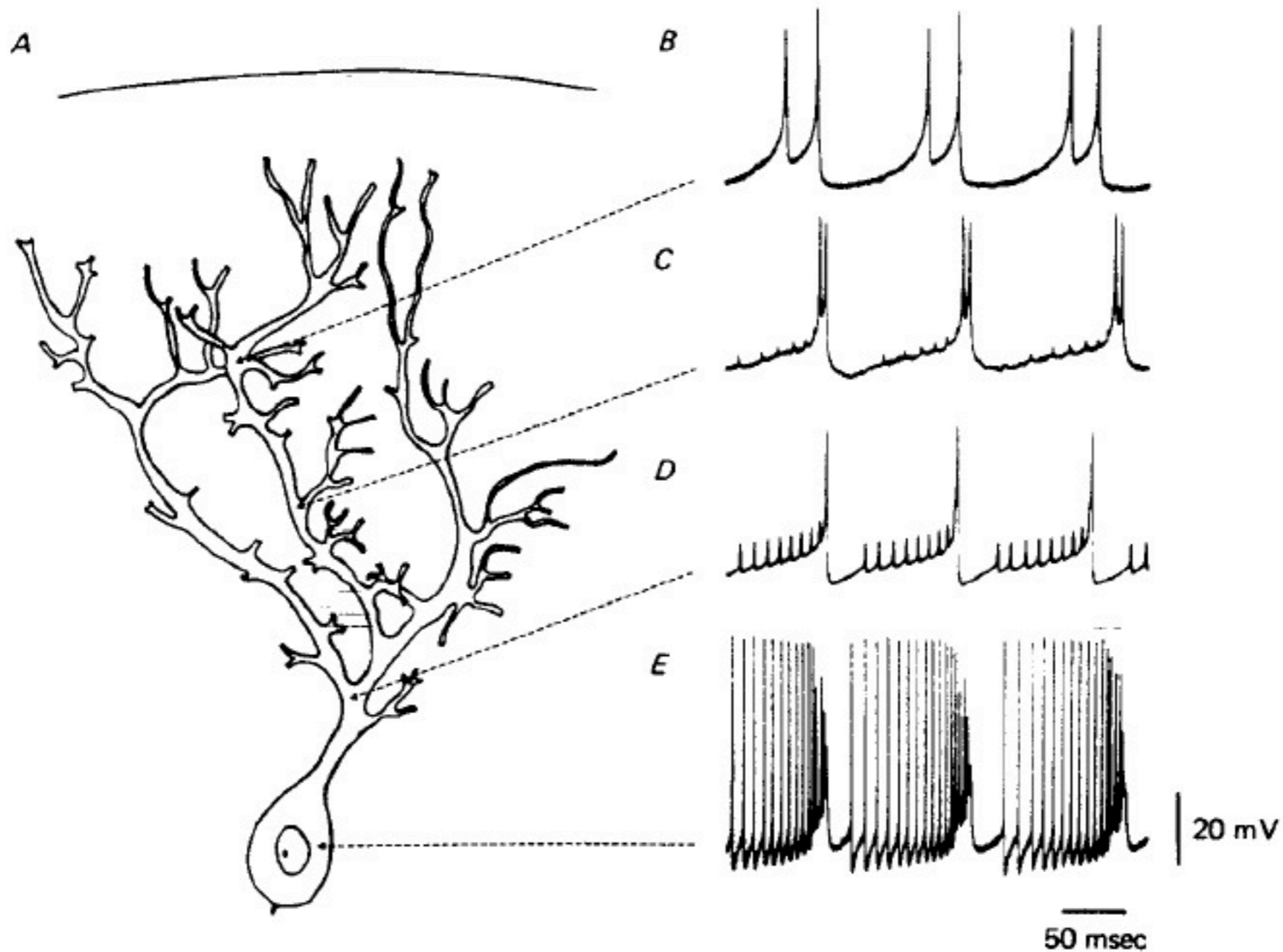


Detailed compartmental models of single neurons:  
Large-scale differential equation models



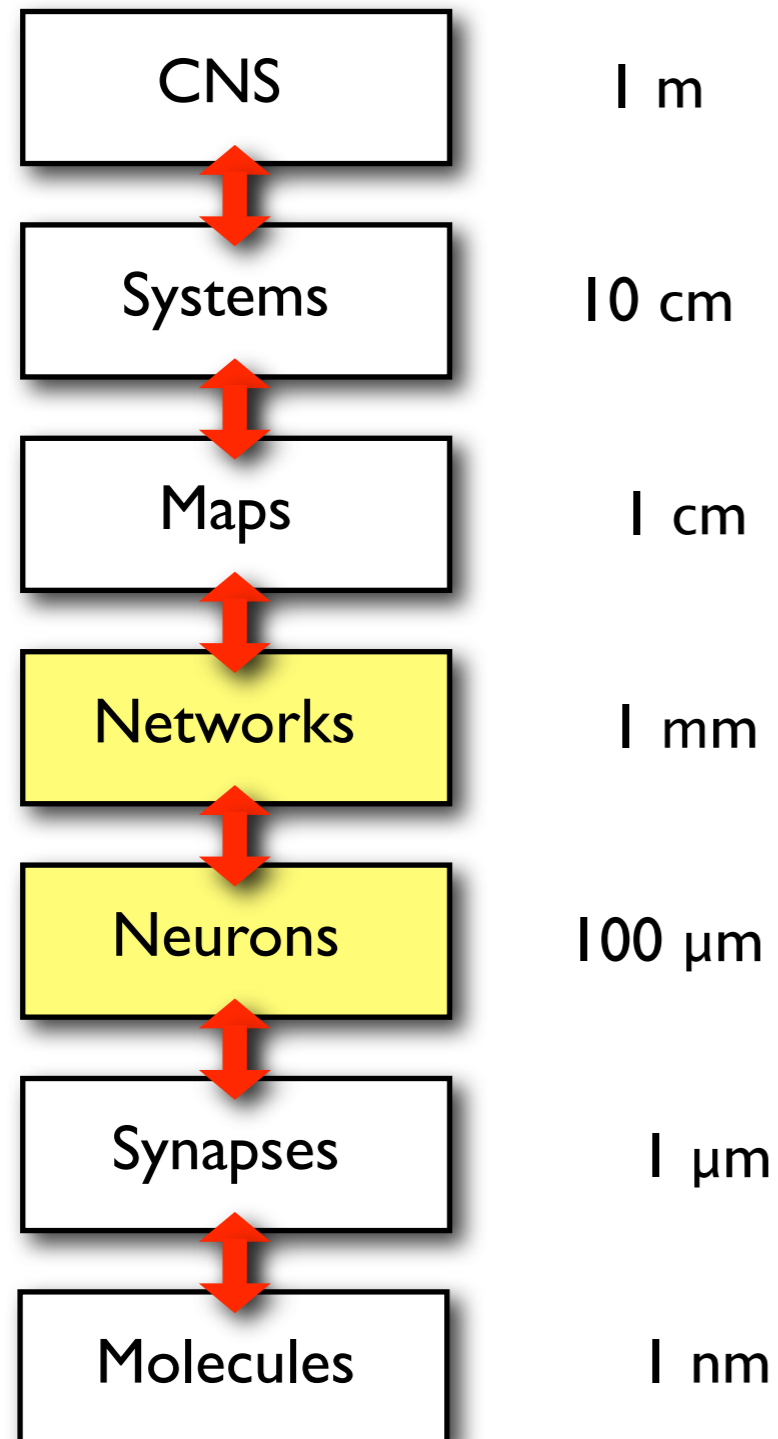
# Reconstructing neurons

## Simulating the membrane potential



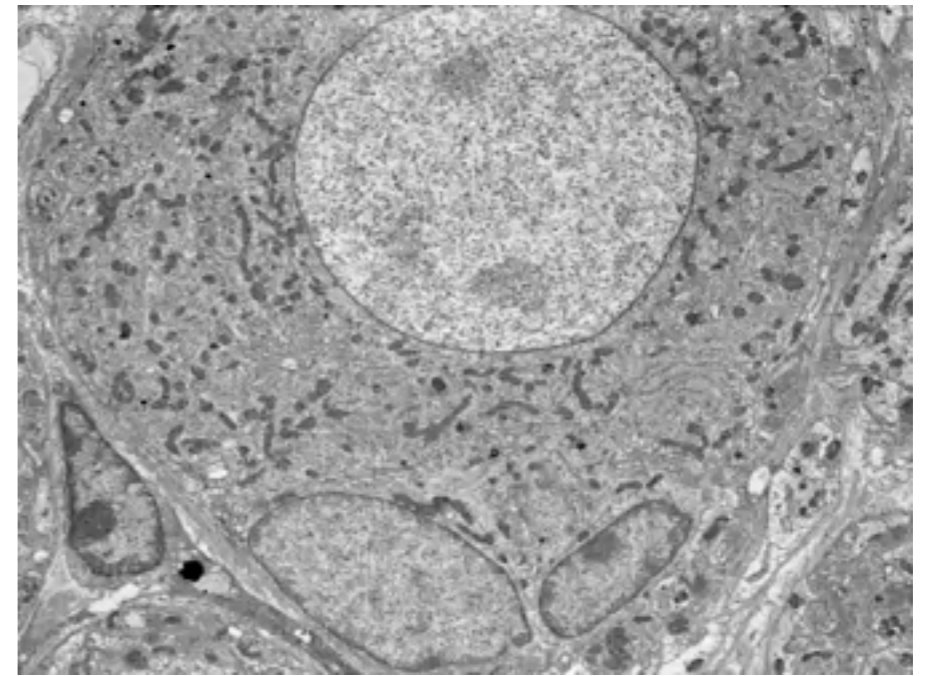
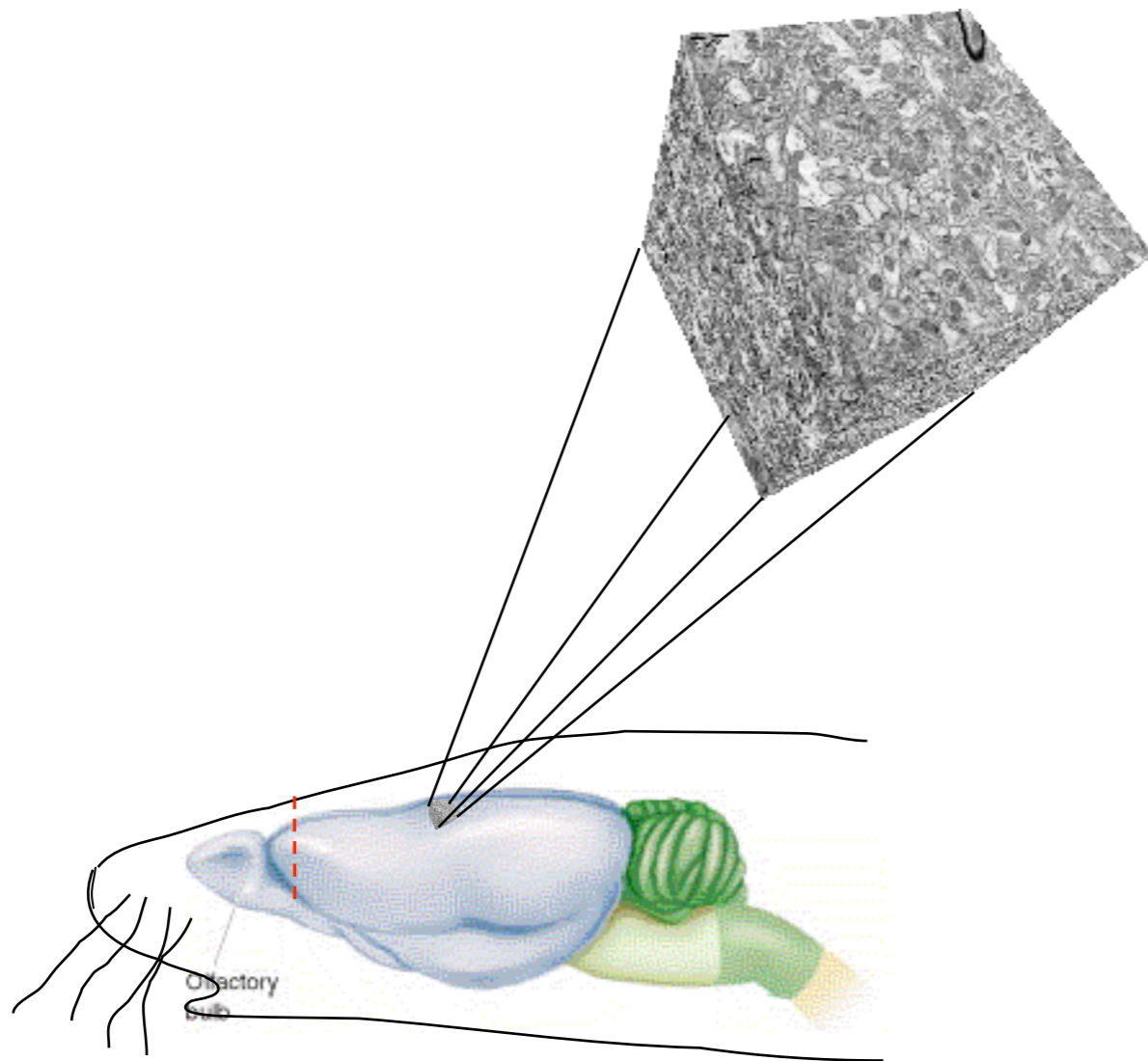
Llinas & Sugimori (1980)

# The quest for mechanisms: Constructing systems from parts



# Reconstructing circuits

## Serial Blockface Scanning Electron Microscopy



courtesy of W.Denk

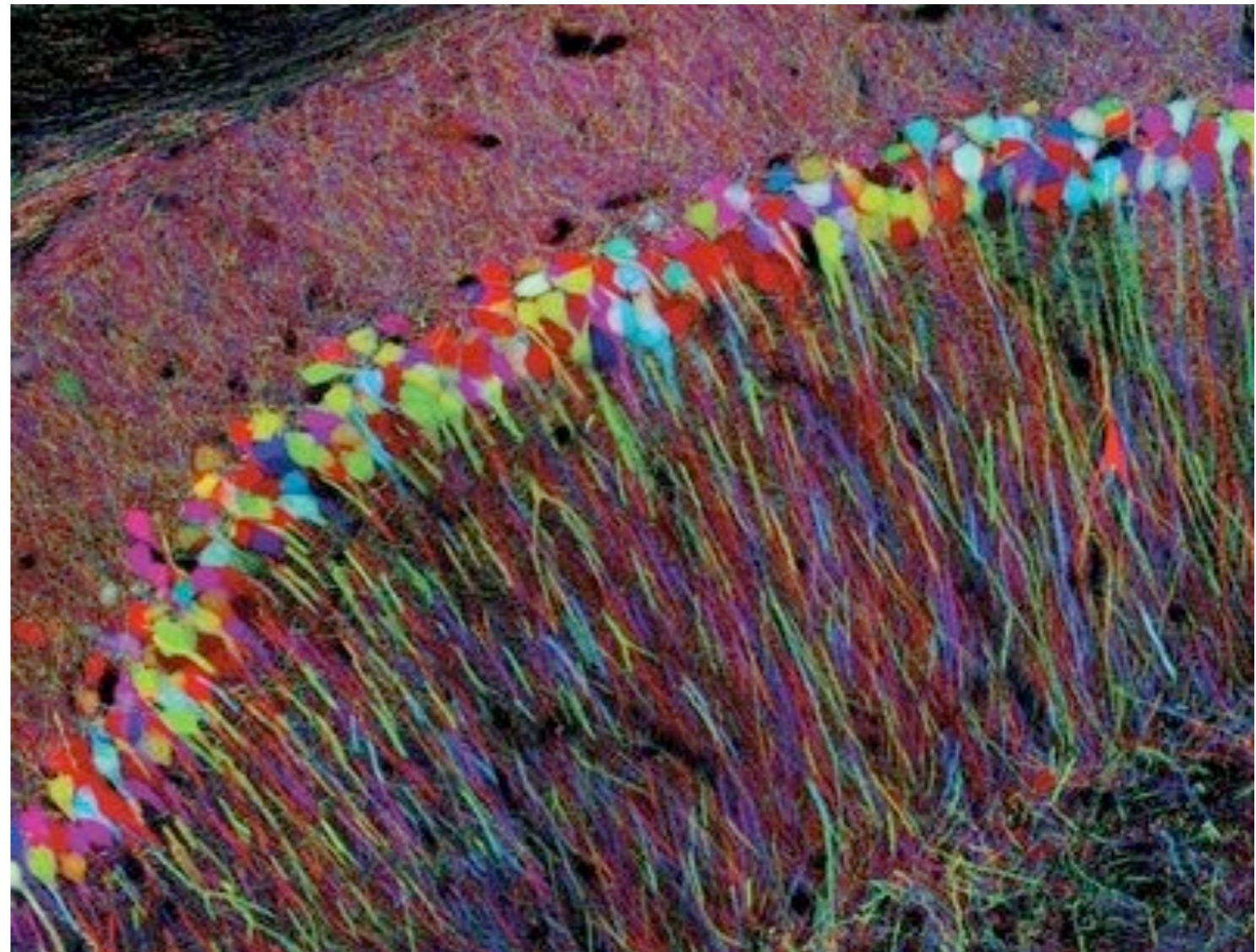


# Reconstructing circuits

## The connectome

Scan brain slices and  
reconstruct the circuit...

but: the devil is in the  
details and when it comes  
to connectivity, details  
matter!

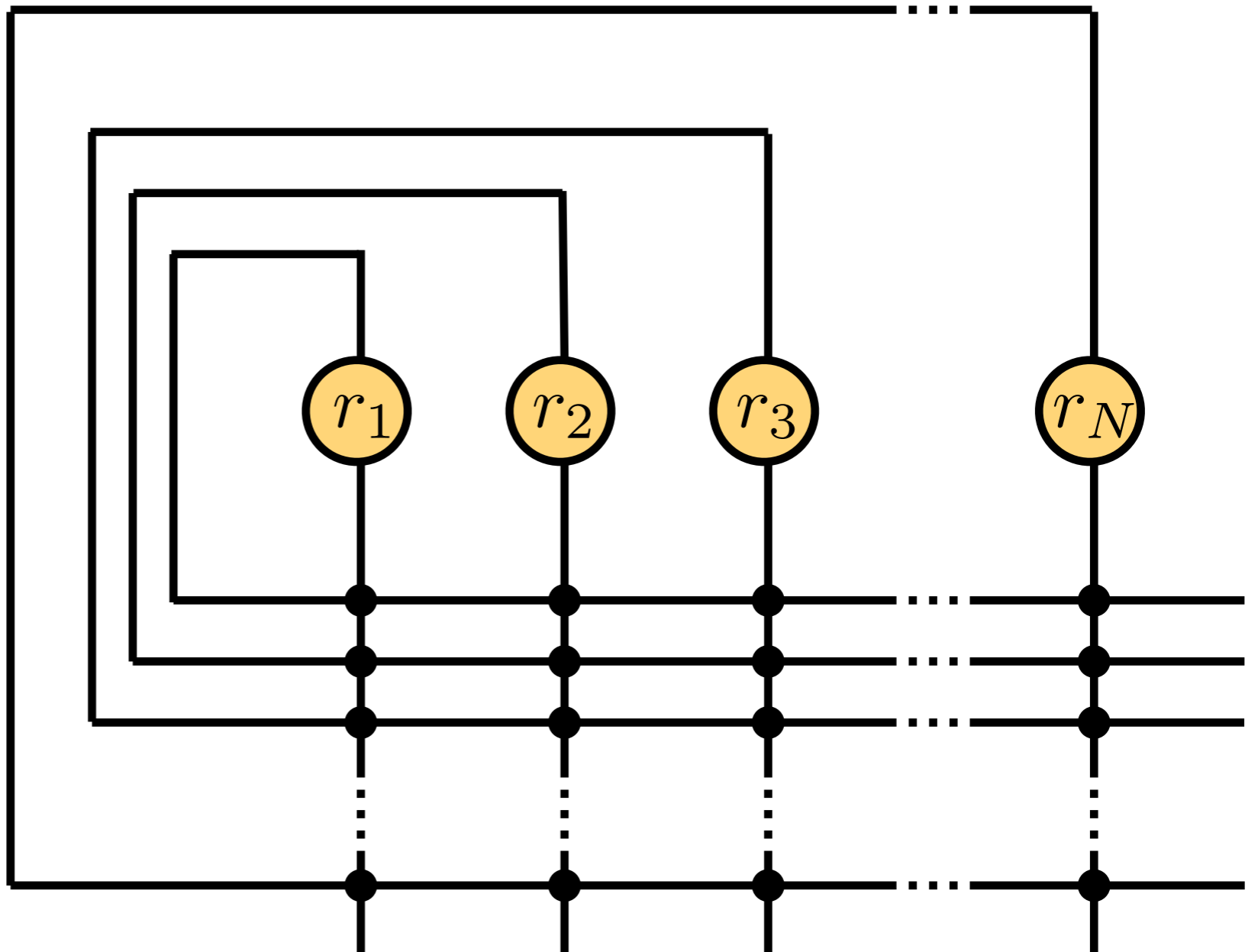


<http://connectomes.org/>

# Theory of neural networks

Neurons, synapses  network activity

$$\dot{r}_i = -r_i + f\left(\sum_{j=1}^N w_{ij} r_j + I_i\right)$$



# Network dynamics largely determined by connectivity

$$\dot{r}_i = -r_i + f\left(\sum_{j=1}^N w_{ij} r_j + I_i\right)$$

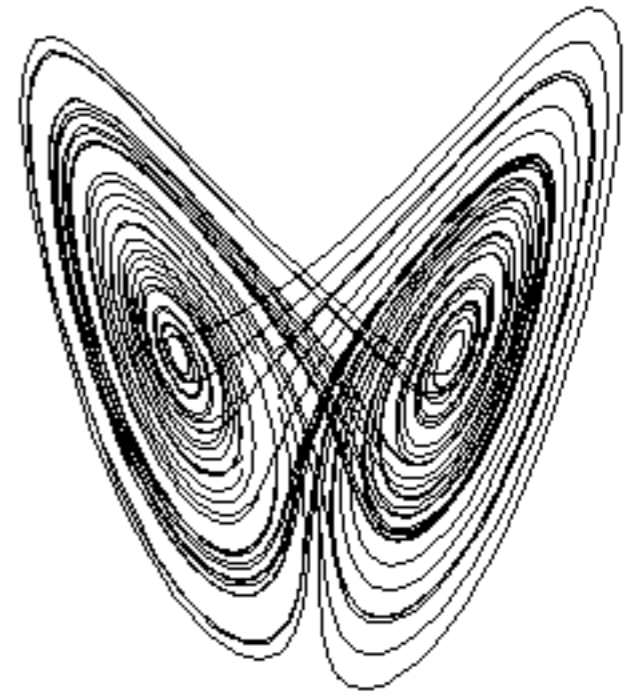
Possible dynamics:

- stable/ unstable fixed points
- limit cycles
- chaotic attractors

Note: different attractors can co-exist  
in different parts of the state space!

For  $N \rightarrow \infty$

- neural networks can compute anything

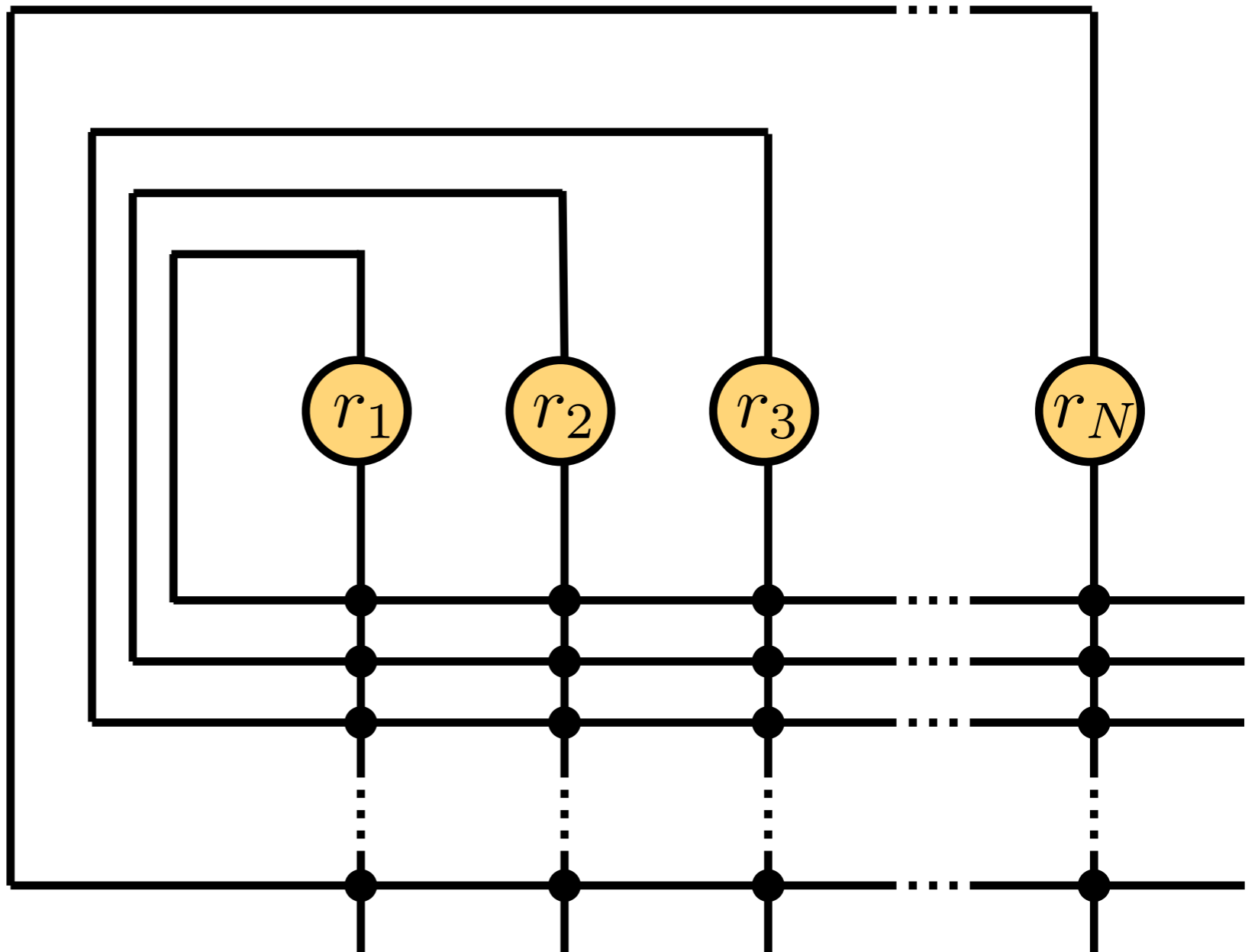


# (Statistical) theory of neural networks

Neurons, synapses  network activity

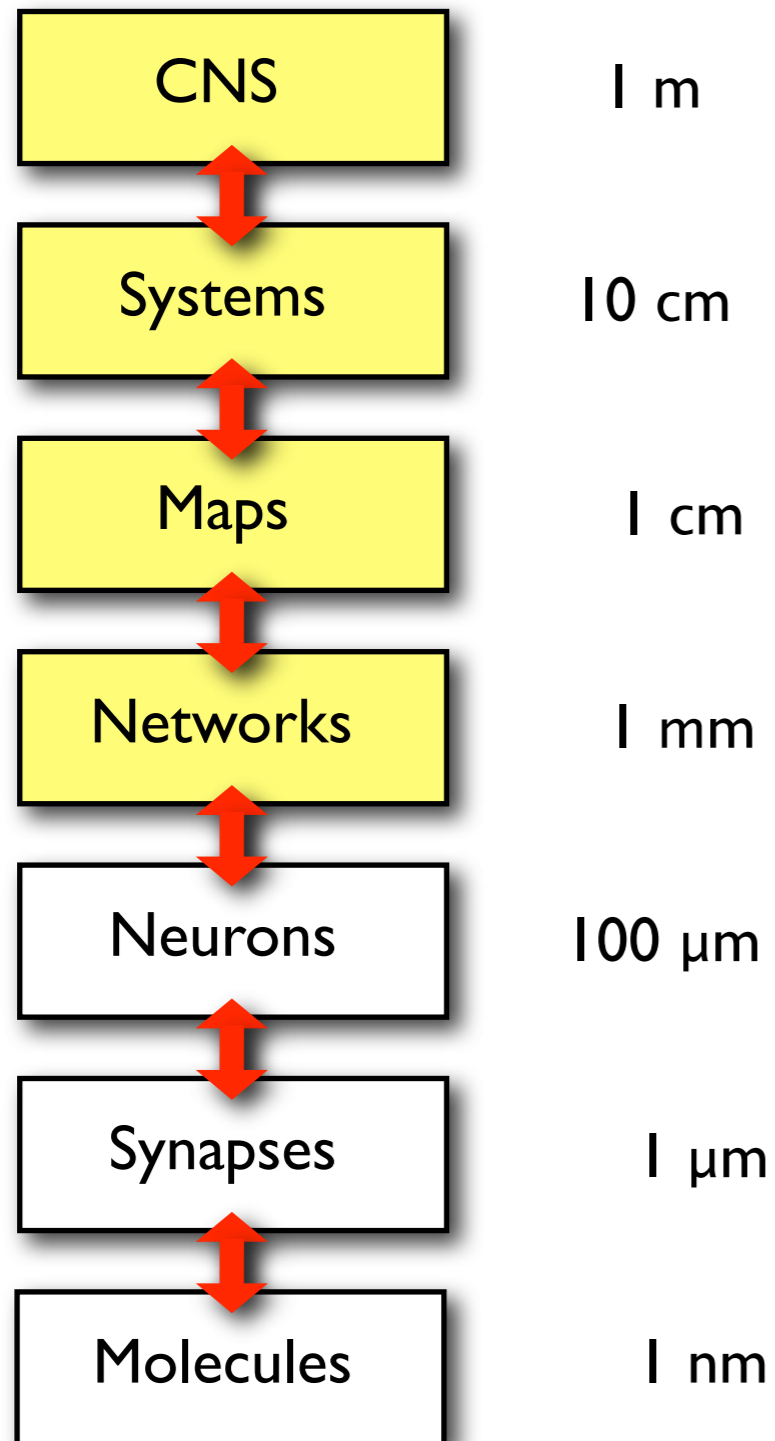
Under what conditions do you get

- only fixed points
- synchronous activity
- asynchronous activity
- Poisson spike trains
- oscillations
- spatial patterns
- ...





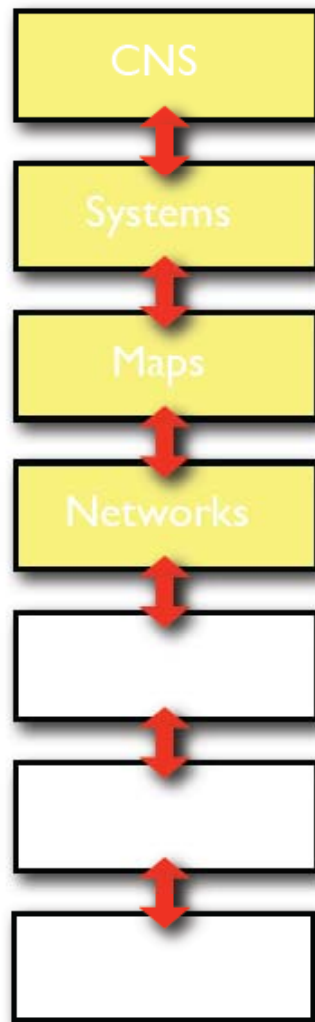
# The quest for mechanisms: Constructing systems from parts





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# The quest for mechanisms: Constructing systems from parts

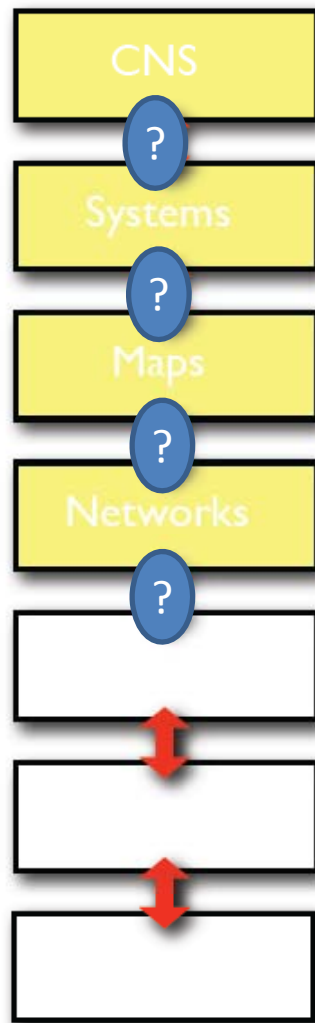


Blue Brain project?



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# The quest for mechanisms: Constructing systems from parts

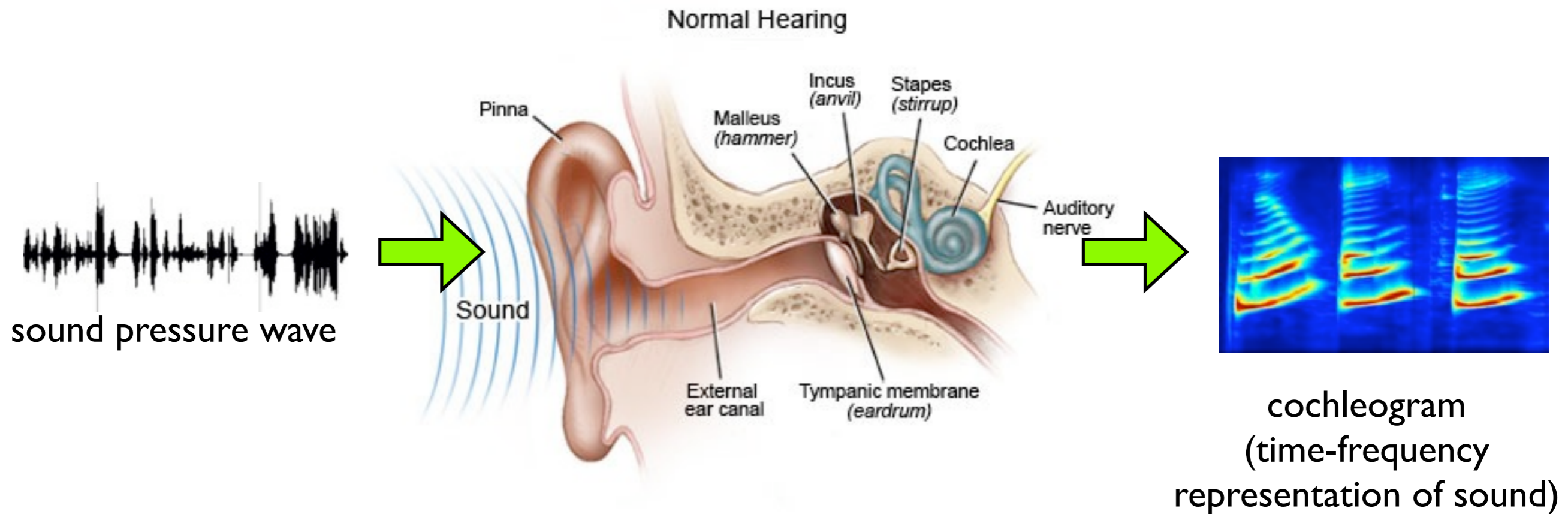


# A computer science approach

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## Study the computational problems

# Computation: manipulating information



# Representation of information, more or less lossy

Example music:

sheet notes



Sound



CD



Language

The other day, I heard this cool jazz CD with this drummer...

# Why represent information differently?

Example numbers:

XXIII

23

00010111

Roman System

Decimal System

Binary System

# Representations allow for easier algorithms

Example numbers:

XXIII

23

00010111

in ...?

in multiples of 10

in multiples of 2

Can you add these numbers?

29  
+ 33  
-----

00011101  
+ 00100001  
-----

XXIX  
+ XXXIII  
-----

# Representations allow for easier algorithms

Example numbers:

XXIII

23

00010111

in ...?

in multiples of 10

in multiples of 2

Can you add these numbers?

29  
+ 33  
-----  
62

00011101  
+ 00100001  
-----

XXIX  
+ XXXIII  
-----



# Representations allow for easier algorithms

Example numbers:

XXIII

23

00010111

in ...?

in multiples of 10

in multiples of 2

Can you add these numbers?

29  
+ 33  
-----  
62

00011101  
+ 00100001  
-----  
00111110

XXIX  
+ XXXIII  
-----

# Representations can ease certain computations

Example numbers:

XXIII

23

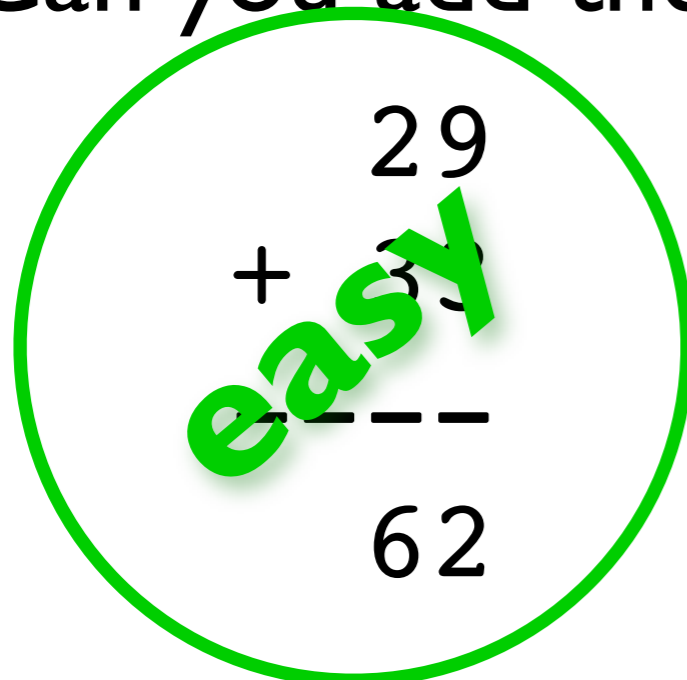
00010111

in ...?

in multiples of 10

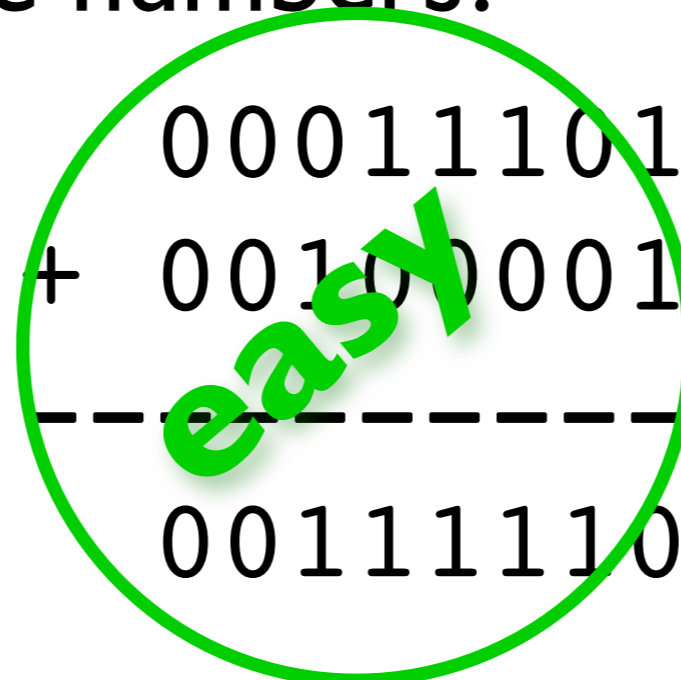
in multiples of 2

Can you add these numbers?



A green circle containing a simple decimal addition problem: 29 plus 33 equals 62. The word "easy" is written in green across the problem.

$$\begin{array}{r} 29 \\ + 33 \\ \hline 62 \end{array}$$



A green circle containing a binary addition problem: 00011101 plus 00100001 equals 00111110. The word "easy" is written in green across the problem.

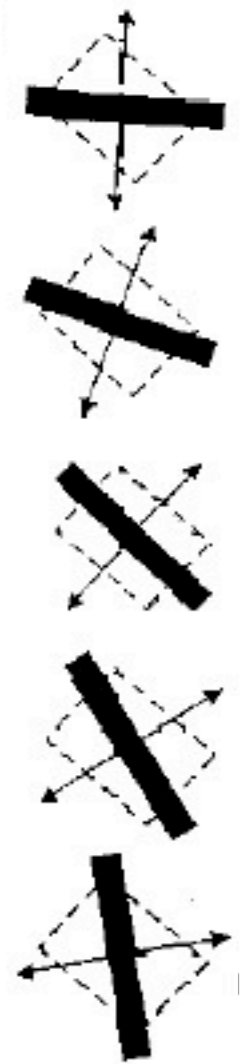
$$\begin{array}{r} 00011101 \\ + 00100001 \\ \hline 00111110 \end{array}$$



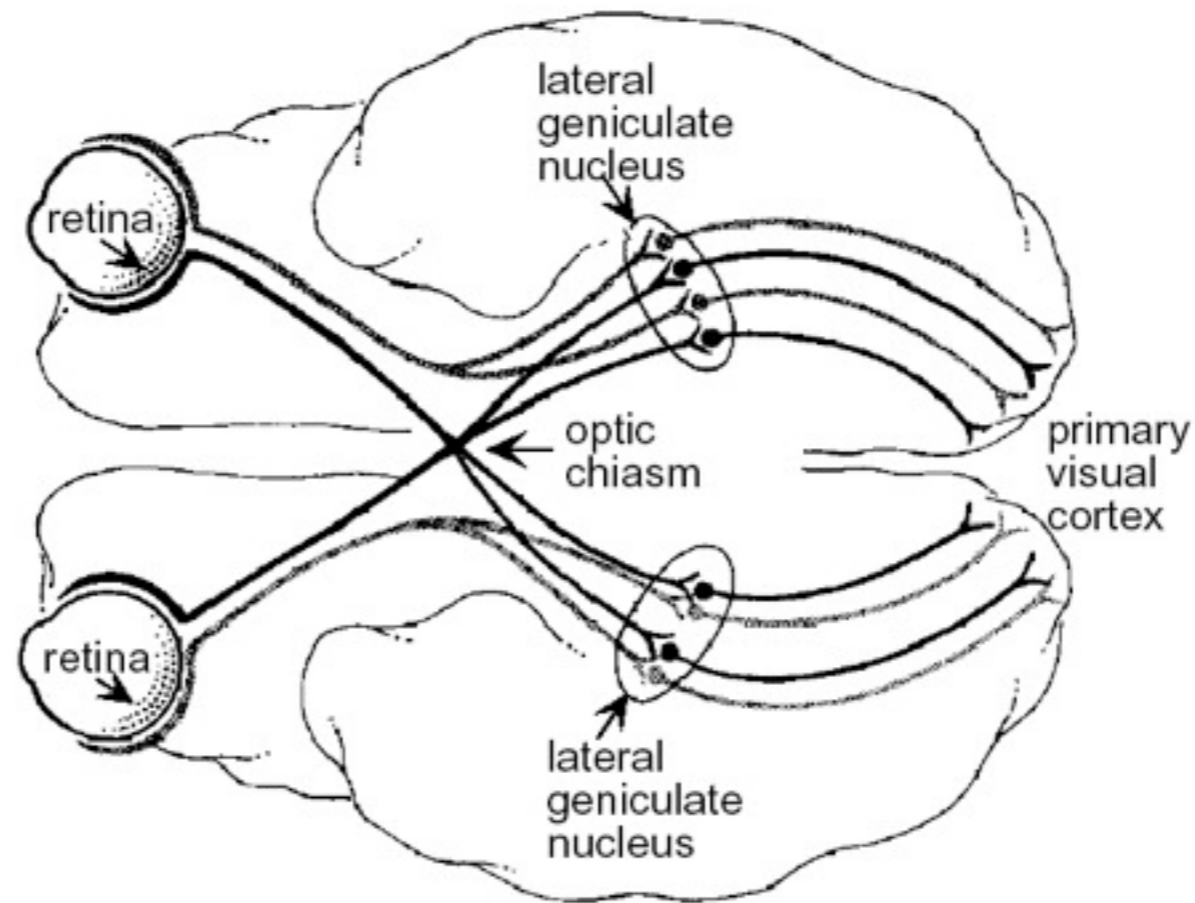
A red circle containing a Roman numeral addition problem: XXIX plus XXXIII. A dashed line is drawn below the numbers, and the word "difficult" is written in red across the problem.

$$\begin{array}{r} XXIX \\ + XXXIII \\ \hline \end{array}$$

# Most famous example: “edge detectors” in visual system

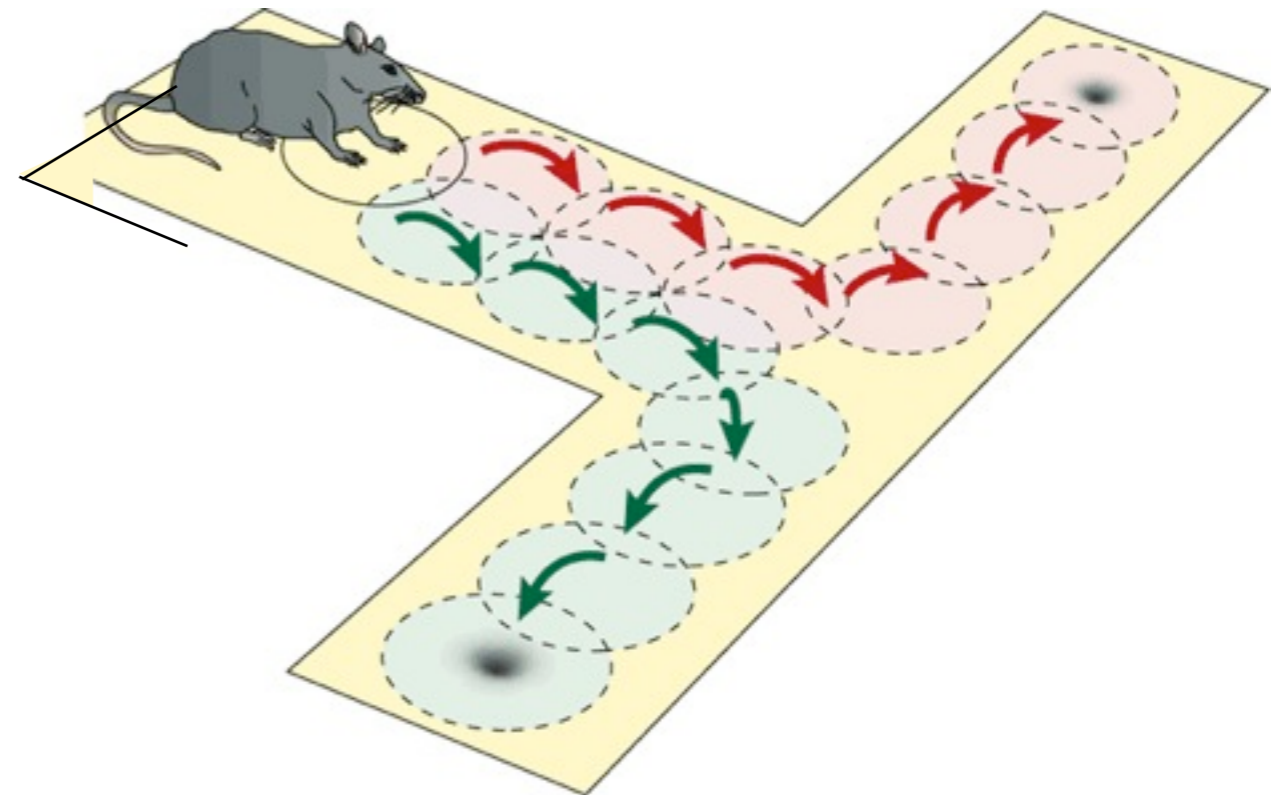


Stimulus:  
black bar

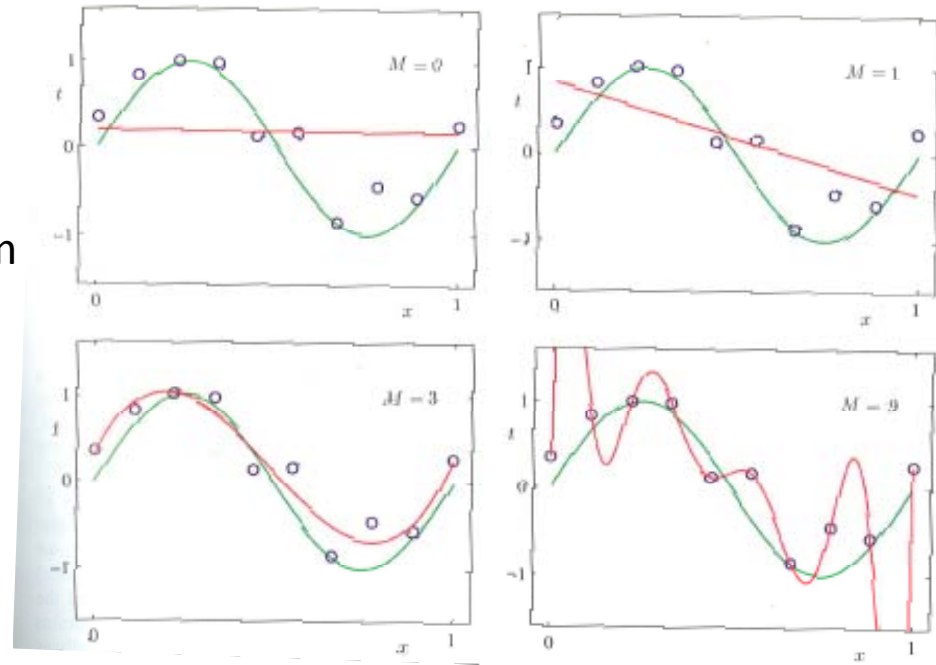
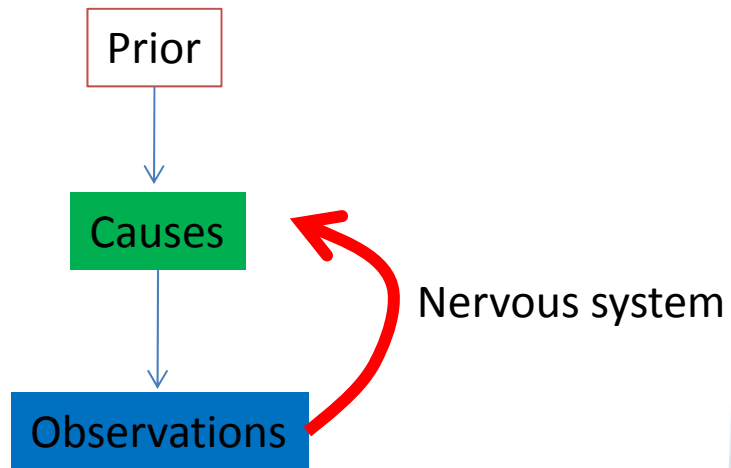


Activity of  
a neuron in V1

# Another famous example: Place cells in the hippocampus

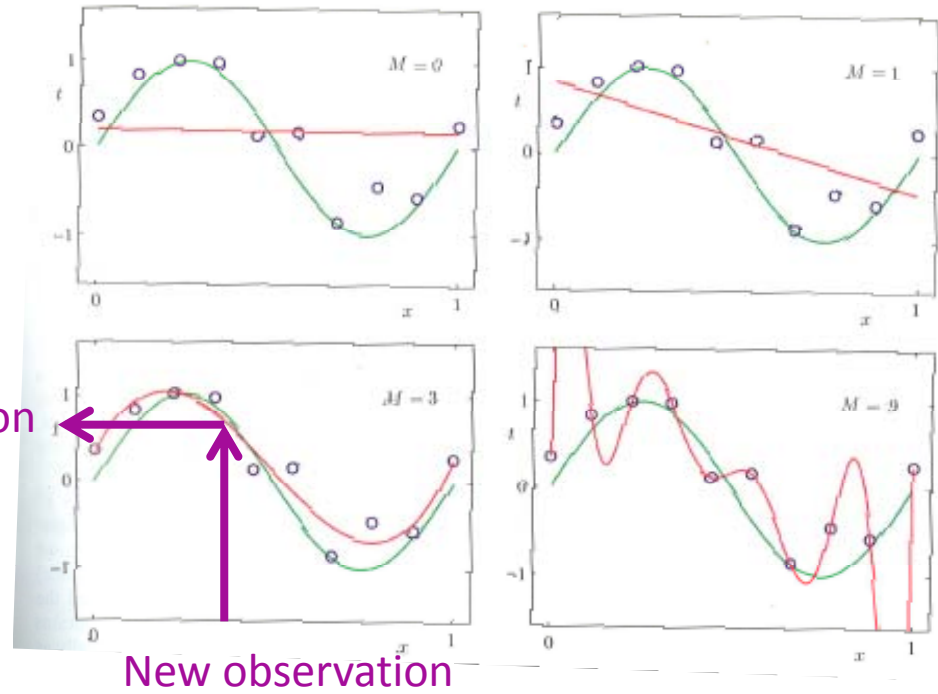
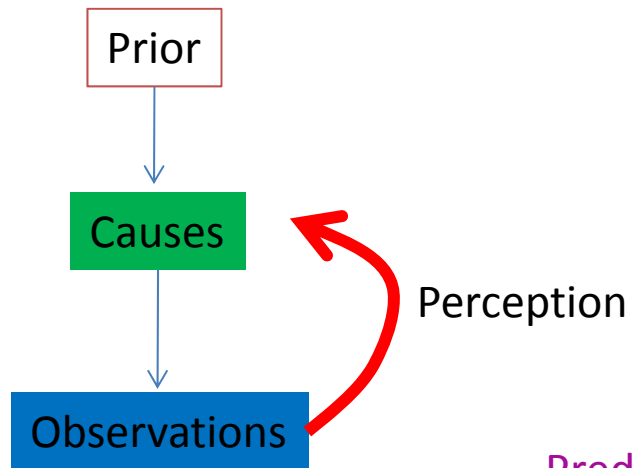


# Understanding cognition. What is the problem?



Machine learning

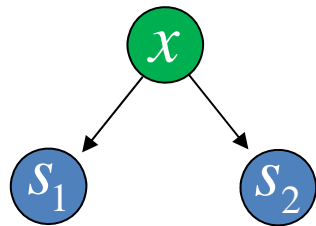
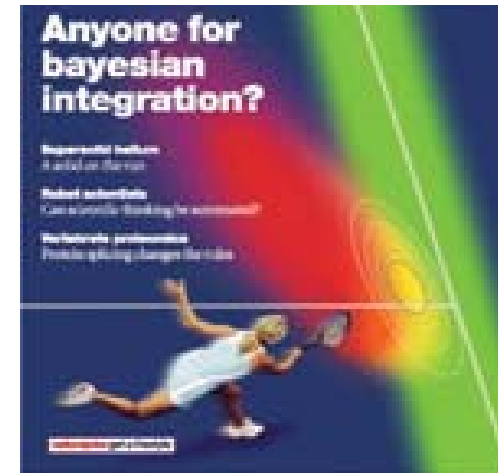
# Understanding cognition. What is the problem?



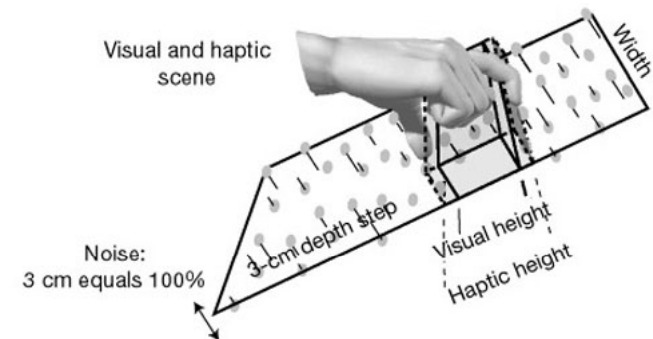
Machine learning

# Example: integrating information from multiple sources

Kording and Wolpert, 2004.



Van Beers, Sittig and Gon, 1999, Ernst and Banks 2002



# Studying representations in the brain

## Experimental work

- perceptual representations:  
vision, audition, olfaction, etc.
- representation of motor variables
- “higher-order” representations:  
decisions  
short-term memory  
rewards  
dreams  
uncertainty  
... you name it ...

## Theoretical work

- Quantifying information content  
quest for the neural code,  
information theory, discriminability, ...
- Understanding the computational  
problems: object recognition, sound  
recognition, reward maximization



# What we understand now

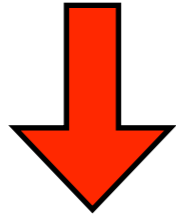
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very little

# What we understand now

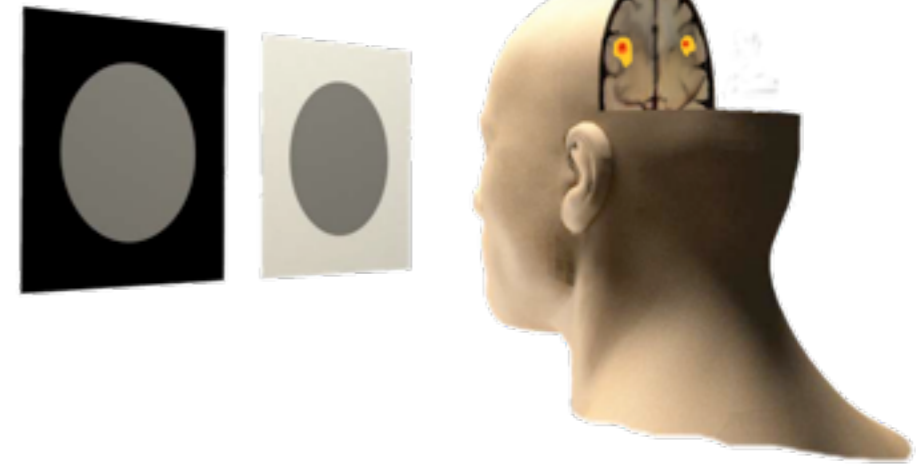
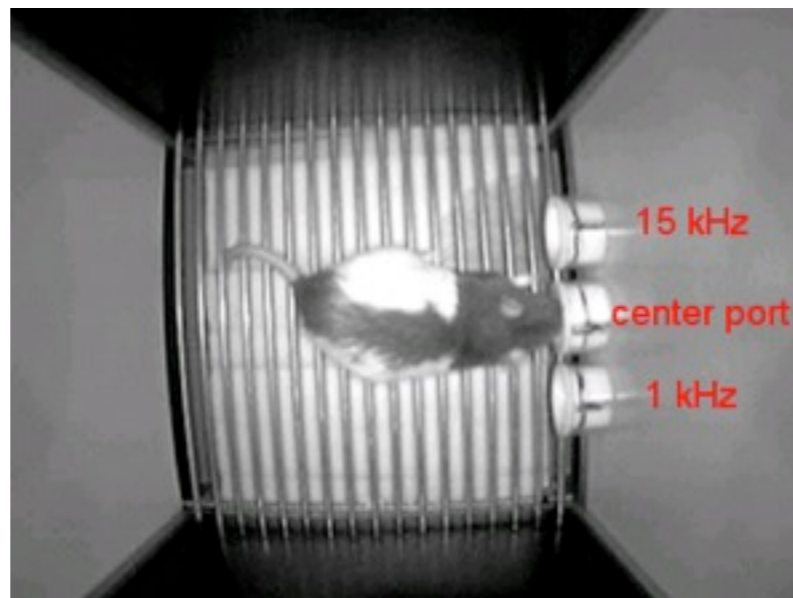
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very little



# What we need

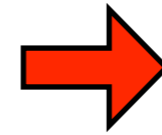
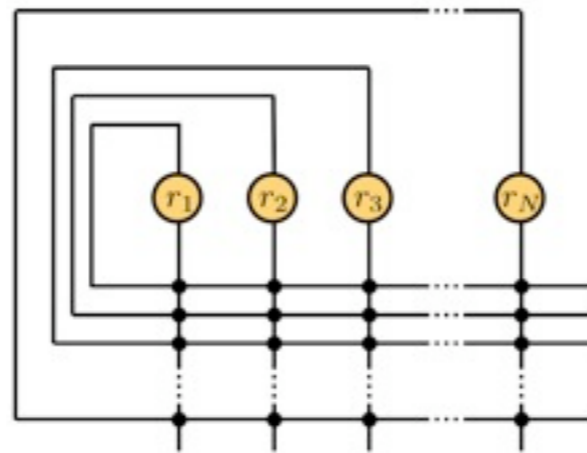
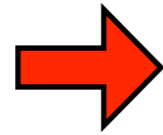
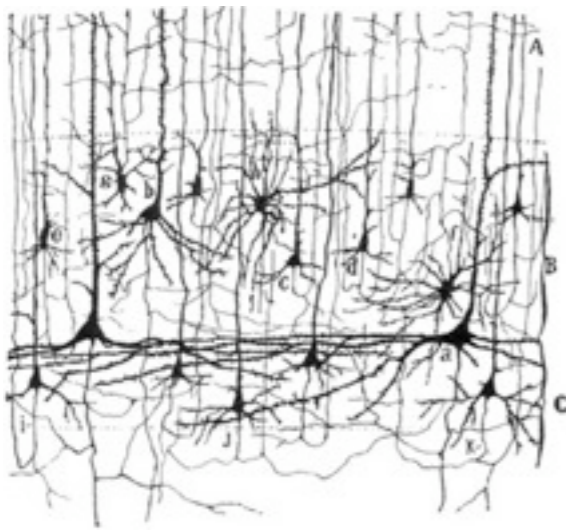
- biologists
- psychologists



- to probe the brains of animals and humans
- to design and carry out clever experiments
- to investigate and quantify human and animal behavior

# What we need

- physicists, computer scientists, engineers, etc.



$$\dot{r}_1 = -r_1 + f\left(\sum_{j=1}^N w_{1j}r_j + E_1\right)$$
$$\dot{r}_2 = -r_2 + f\left(\sum_{j=1}^N w_{2j}r_j + E_2\right)$$

- to formulate mathematical theories of information processing
- to create biophysical models of neural networks

# Teaching in the Cogmaster

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## Computational Neuroscience

# Core classes

- AT2: Atelier Comput. Neuroscience- V Benichoux. S2
- CO6: Introduction to Comput. Neuroscience – R Brette, B Gutkin, S Deneve. S2
- CA6(a): Theoretical Neuroscience- JP Nadal, N Brunel, R Brette, G Mongillo. S1
- CA6(b): Seminar in Quantitative Neuroscience- s Deneve, B Gutkin. S1
- CA6(c): Machine learning applied to cognition- F Bach, S Deneve. S2

# Many more classes available!!

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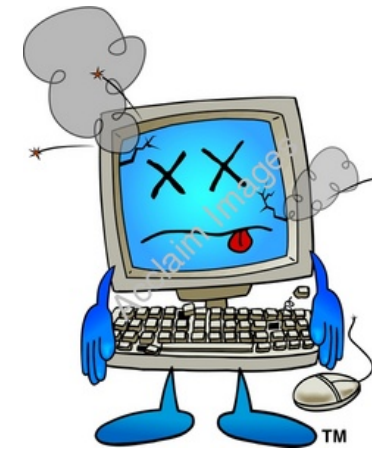
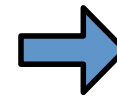
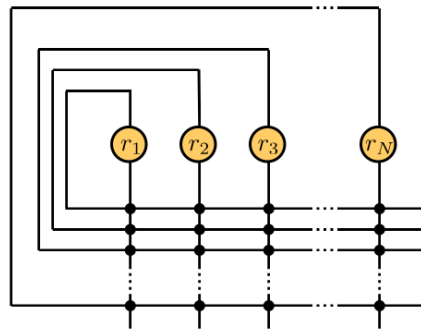
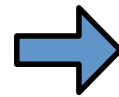
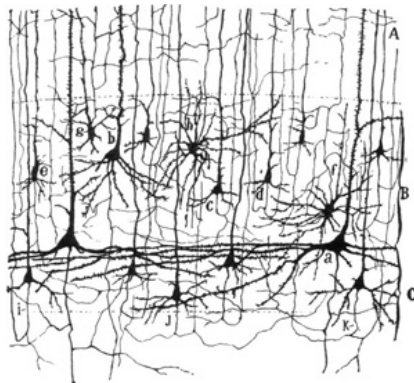
see cogmaster website!!

contact us!!



# MI AT2

# Atelier théorique neuromodélisation



## What you need

- Basic math skills  
(ask if you are uncertain!)

## What you get

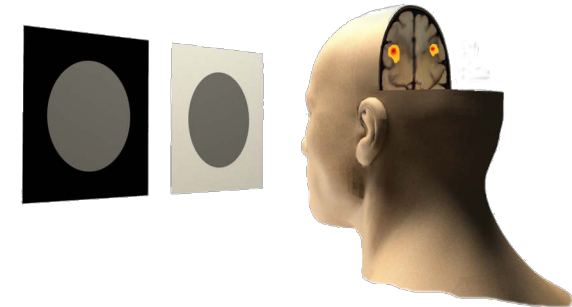
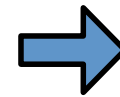
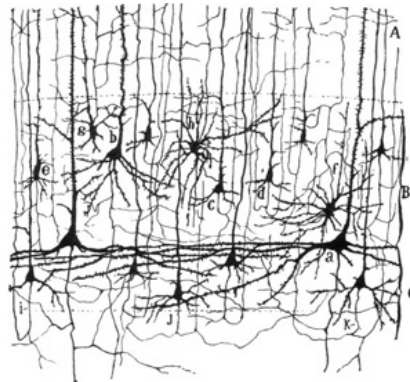
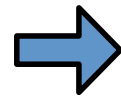
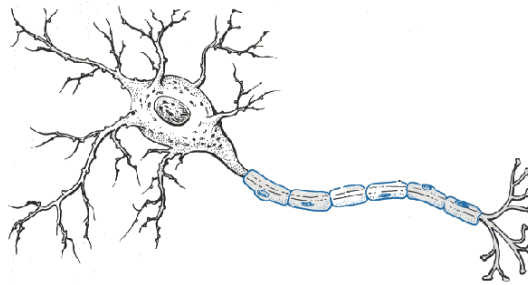
- Education in an exciting field!
- 4 ECTS

## Validation

- 100% course exercises



Boris Gutkin/Sophie Deneve/Romain Brette



## Neurons

- Membrane voltage
- Action potentials
- Computations

## Networks

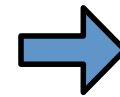
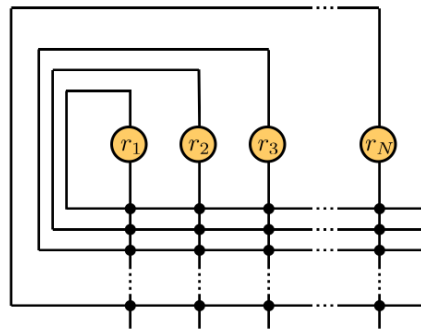
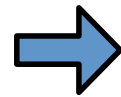
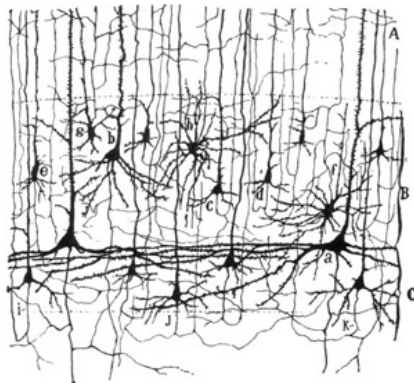
- Attractors
- Associative memory
- Decision-making
- Sensory processing

## Behavior

- Psychophysics
- Reinforcement Learning
- Neuroeconomics



Boris Gutkin/Sophie Deneve/Romain Brette



$$\dot{r}_1 = -r_1 + f\left(\sum_{j=1}^N w_{1j}r_j + E_1\right)$$

$$\dot{r}_2 = -r_2 + f\left(\sum_{j=1}^N w_{2j}r_j + E_2\right)$$

## What you need

- Basic math skills  
(ask if you are uncertain!)

## What you get

- Education in an exciting field!
- 6 ECTS

## Validation

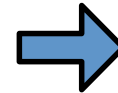
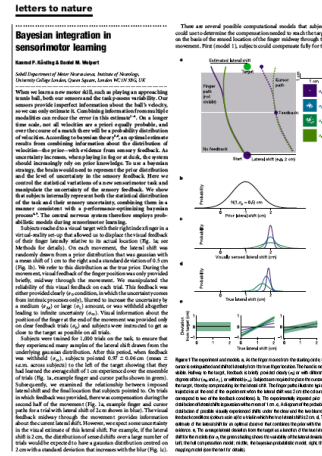
- 100% exam

# MI-M2 Seminar / Journal Club

## CA6b Quantitative Neuroscience



Boris Gutkin/Vincent Hakim/Sophie Deneve/Romain Brette



### What you need

- Basic math skills  
(ask if you are uncertain!)

### What you get

- State-of-the-art science
- Learn how to give a talk
- 4 ECTS

### Validation

- 50% talk
- 50 % course participation

# Theoretical Neuroscience Course

Romain Brette, Nicolas Brunel, Gianluigi Mongillo, Jean-Pierre Nadal

TA: Alexis Dubreuil

## **1 Introduction**

Lecture 1 (Sept 29) NB

## 2 Basic tools

### 2.1 Neurons

Lecture 2 (Oct 6) RB

- Spike trains: the Poisson process
- Neuronal electricity (electrodifusion, equivalent electrical circuit, the membrane equation).
- The integrate-and-fire model (definition, firing rate, reliability of spike timing).
- The Hodgkin-Huxley model (voltage-gated channels, HH model, threshold in a 1D approximation, refractory period)
- Variations around the IF model (perfect integrator, quadratic, exponential, Izhikevich, adaptive exponential)
- Dendrites (linear cable theory, stationary response, Green function, cable equation on the dendritic tree)

## 2.2 Synapses

### Lecture 3 (Oct 13) GM

- Basic physiological facts about chemical synaptic transmission.
  - Neurotransmitter release and post-synaptic receptor machinery.
  - The Katz synapse: quantal release, role of calcium, stochasticity.
  - The binomial model.
- Short-term synaptic plasticity
  - The Tsodyks-Markam (TM) model for STP
  - Quantal interpretation of the TM model
  - Stochastic STP model
  - Statistics of post-synaptic response as a function of pre-synaptic activity
  - Filtering properties of STP
- Long-term synaptic plasticity
  - Phenomenological models of STDP
  - Role of post-synaptic calcium in STDP
  - A simple phenomenological model of a bistable synapse



## 2.3 Learning

Lecture 4 (Oct 20) JPN

- Different types of learning : supervised, unsupervised, reinforcement learning
- Supervised learning : perceptron
- Hebbian unsupervised learning : the Oja model; link with neural coding

## 2.4 Coding

Lecture 5 (Oct 27) JPN

- Basic tools (Shannon information, Fisher information)
- Optimal tuning curve : Laughlin's fly
- Population coding
- Decoding, decision-making: reaction times

## 2.5 Networks

Lecture 6 (Nov 10) NB (Rate models, Network architectures)

- Large-scale anatomy
- Architecture of neuronal microcircuits
- Rate models

Lecture 7 (Nov 17) NB (Networks of spiking neurons)

- Local cortical networks: anatomy, physiology
- Low rate irregular activity
  - Asynchronous states in networks of spiking neurons
  - The balanced network model
  - Networks of LIF neurons
- Oscillations
  - Overview of oscillations in the nervous system
  - Overview of mechanisms
  - Oscillations in networks of LIF neurons

## **3 Models of specific systems**

### **3.1 Retina**

Lecture 8 (Nov 24)

### **3.2 Primary visual cortex**

Lecture 9 (Dec 1)

### **3.3 Auditory system**

Lecture 10 (Dec 15)

### **3.4 Association cortex**

Lecture 10 (Dec 8)

### **3.5 Hippocampus**

Lecture 11 (Jan 5)

## **3.6 Cerebellum**

Lecture 13 (Jan 12)

# CA6(c) Machine learning applied to cognition

Enseignants: Francis Bach, Sophie Deneve S2

## 1. Probabilistic methods.

Prior, posterior, likelihood, Generative models, maximum likelihood.  
Application: Cue combination in behavior and cortical networks.

## 2. Representational learning (unsupervised learning)

Information maximization, Principle component analysis (PCA),  
Independent component analysis (ICA), sparse coding.  
Application: sensory receptive fields.  
Methods: PCA, ICA, CCA, sparse coding

## 3. Supervised learning (classification/regression).

Linear classifiers, Gaussian mixtures, support vector machines (linear and non-linear).  
Applications: Reading out the mind. Object recognition.  
Methods: SVM, logistic, k-NN, Cart, neural networks

## 4. Interpolation.

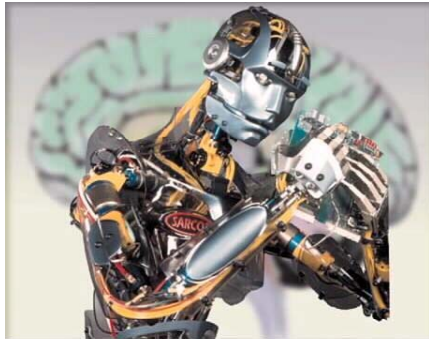
Gaussian processes, density estimation, Expectation/maximization.  
Application: Unsupervised learning in humans and animals.  
Methods: Parzen, k-means, GMM

# M2 CA6(c)

# Machine learning applied to cognition

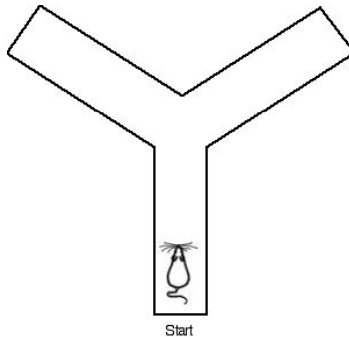


F Bach, G Obozinski, N le Roux, S Deneve



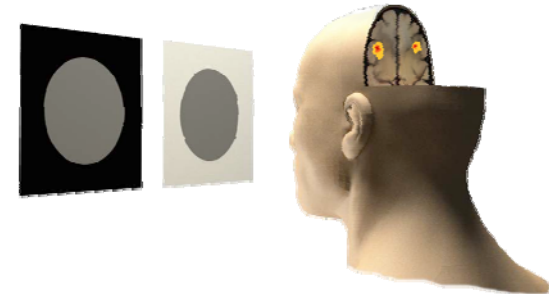
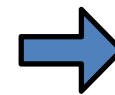
## Learning in machine

- Bayesian networks
- Sparse coding
- SVM



## Learning in Behavior

- Unsupervised
- Supervised
- Hierarchy
- Internal models



## Neural implementation

- Receptive fields
- Sensory representation
- Neural code



Brain machine interface

# Computational Neuroscience Research in the Cogmaster and Beyond

---

ENS: [Group for Neural Theory](#)

(Sophie Deneve, Boris Gutkin, Christian Machens, ...)

ENS: [Equipe Audition](#)

(Romain Brette, Victor Benichoux, ...)

ENS: [Laboratoire de Physique Statistique](#)

(Jean-Pierre Nadal, Vincent Hakim, ...)

Paris V: [Laboratoire de Neurophysique et Physiologie](#)

(Nicolas Brunel, David Hansel, ...)

you can find more labs under:

<http://cogmaster.net>

<http://neurocomp.risc.cnrs.fr>

for internship / stages / Master's thesis: contact the faculty! (email etc.)



# Computational Neuroscience

## Groups, ENS

### **Group for Neural Theory, DEC**

Boris Gutkin

Sophie Deneve

Srdjan Ostrojc

### **Neurocomputation, Equipe Audition, DEC**

Romain Brette

### **Computational Neuroscience, LPS, Physics**

Vincent Hakim

Jean-Pierre Nadal

Rava da Silveira

### **Frontal Lobe Function Group, LNC, DEC**

Etienne Koechlin

### **Neuromathcomp, Dept of Computer Science, ENS**

O Faugeras

# Group for Neural Theory

- Boris Gutkin:
  - Dynamics of Neuronal Activity, Addiction Models, Oscillations in Speech Processing and Memory
- Sophie Deneve:
  - Bayesian Theory of Sensory Processing, Bayesian Theory of Neuronal Dynamics, Computational Psychiatry
- Srdjan Ostrojcic:
  - Models of Oscillatory Dynamics, Models of Sequence learning and decision making



# Neurocomputation, Equipe Audition

- Romain Brette
  - spike-based computation in the auditory system (especially sound localization and pitch perception).
  - spiking neuron models (including threshold dynamics)
  - simulation of spiking neural networks (in particular the Brian simulator)



# Frontal Lobe Function Group, LNC, DEC

- Etienne Koechlin
  - Information value learning in human prefrontal cortex
  - executive and motivational control during decision making



Laboratoire de Physique Statistique (LPS)  
Ecole Normale Supérieure  
24, rue Lhomond – 75005 Paris

Neurosciences computationnelles, biophysique théorique  
*Computational neuroscience, theoretical biology*

<b>Rava da Silveira</b>	<i>theoretical neuroscience</i>
<b>Simona Cocco</b>	<i>theoretical biophysics (DNA, neurons,...)</i>
<b>Vincent Hakim</b>	<i>theoretical biology, theoretical neuroscience</i>
<b>Thierry Mora</b>	<i>theoretical biophysics</i>
<b>Jean-Pierre Nadal</b>	<i>theoretical neuroscience, complex systems</i>
<b>Jacques Ninio</b>	<i>experimental psychophysics, theoretical biology</i>

*Team Complex networks and cognitive systems*

*<http://www.lps.ens.fr/~risc/rescomp/>*

Contacts:

nadal@lps.ens.fr

hakim@lps.ens.fr

# Computational Neuroscience, LPS, Physics

- **Vincent Hakim**
  - Neuronal synchronization, dynamics of neural ensembles
  - Cerebellar processing
- **Jean-Pierre Nadal**
  - Information processing in biological systems
  - Complex systems in cognitive and social sciences
- **Rava da Silveira**
  - computation and adaptation in single neurons
  - coding of information in the brain
  - molecular machinery at synapses



**Laboratory of Neurophysics and Physiology**

**CNRS - Université Paris Descartes**

45 rue des Saints Pères, 75006 Paris



# People

Carl van Vreeswijk



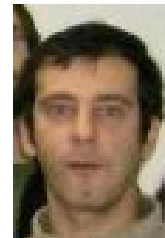
Claude Meunier



David Hansel



Gianluigi Mongillo



Nicolas Brunel





# Research interests

- Single neuron dynamics: C. van Vreeswijk, N.Brunel, C.Meunier
- Network dynamics: C. van Vreeswijk, N.Brunel, D.Hansel, G.Mongillo
- Models of specific systems:
  - Spinal cord (C.Meunier, collaboration with experimental group of D.Zytnicki)
  - Visual cortex (D.Hansel and C.van Vreeswijk, collaboration with experimental group of L.Nowak (Toulouse); N.Brunel, collaboration with experimental group of N.Logothetis (Tubingen))
  - Motor cortex (C.van Vreeswijk, collaboration with experimental group of C.Capaday (Copenhagen))
  - Cerebellum (N Brunel, collaboration with V Hakim, JP Nadal, and experimental groups of B Barbour, S Dieudonné, C Léna (ENS))
  - Basal ganglia (D Hansel, collaboration with experimental groups of T Boraud (Bordeaux) and H Bergman (Jerusalem))

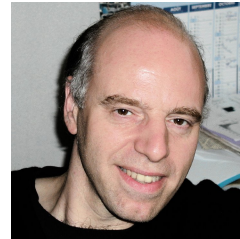
**Laboratory for Computational Neuroscience**  
**Unit de Neurosciences, Information and Complexit (UNIC)**

**CNRS**

91198 Gif-sur-Yvette

# People

Alain Destexhe



Michelle Rudolph



# The articles you have read:

## Neural coding

WT Newsome, KH Britten, JA Movshon  
[Neuronal correlates of a perceptual decision](#)

## Reinforcement Learning

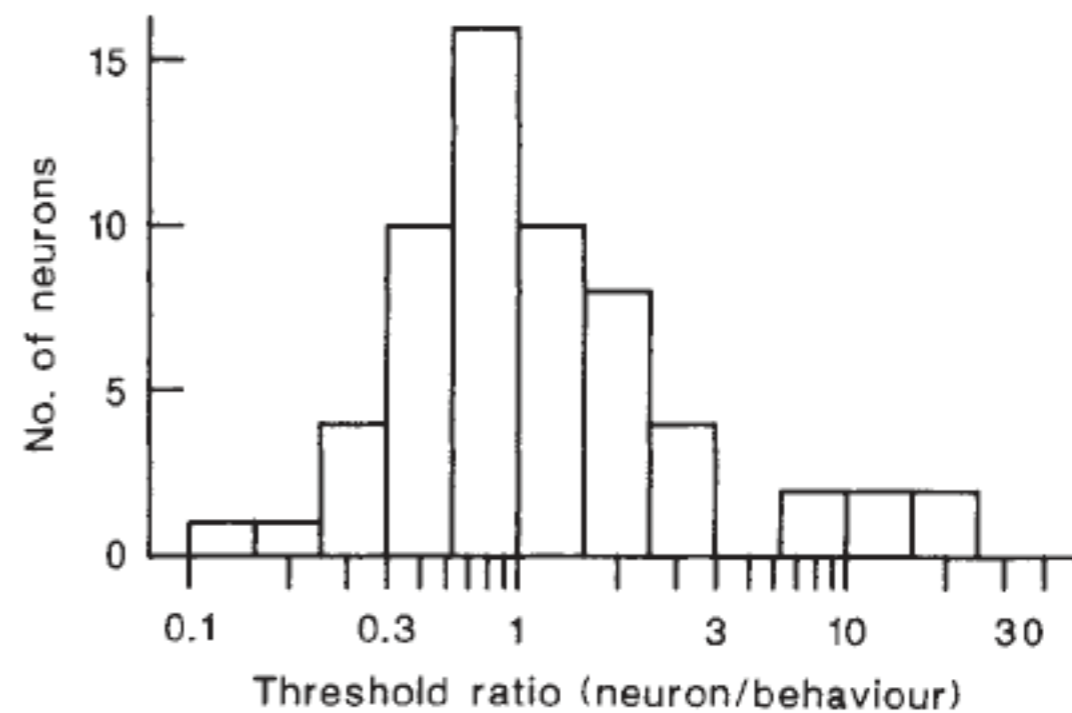
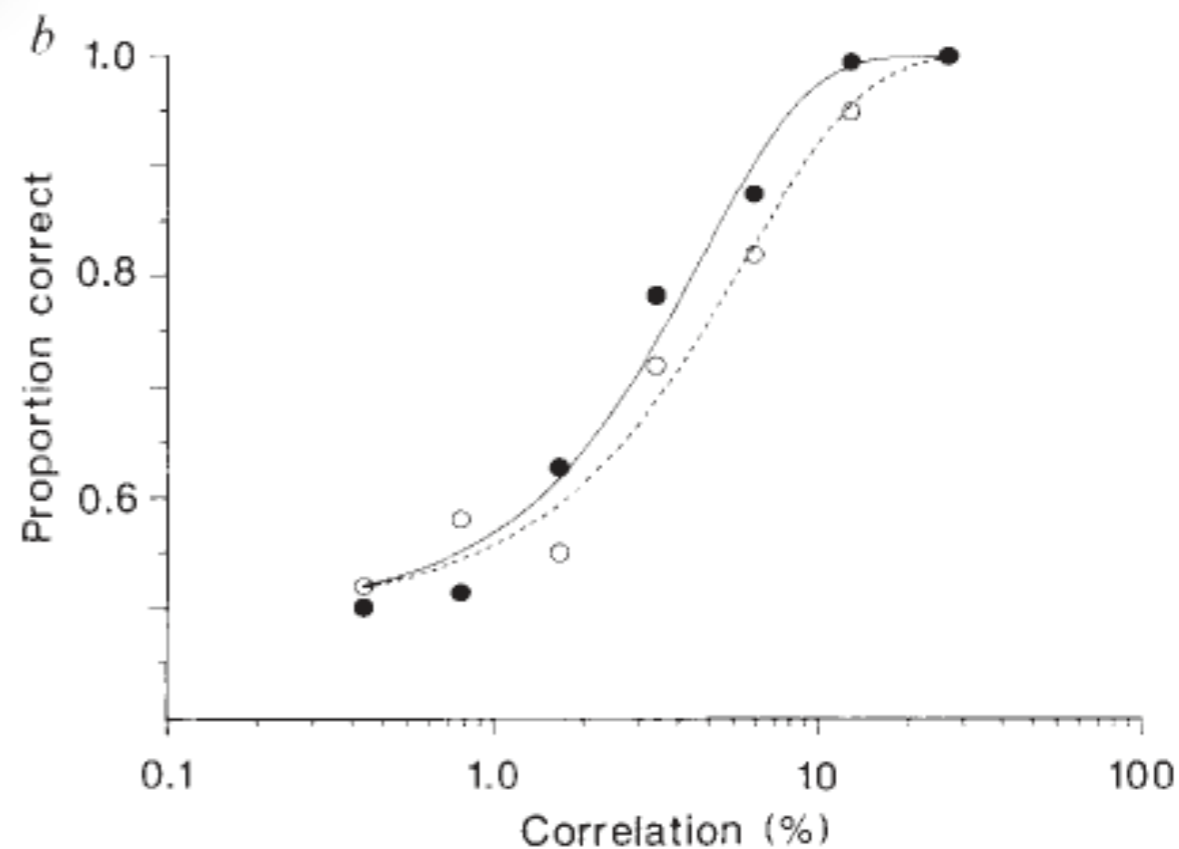
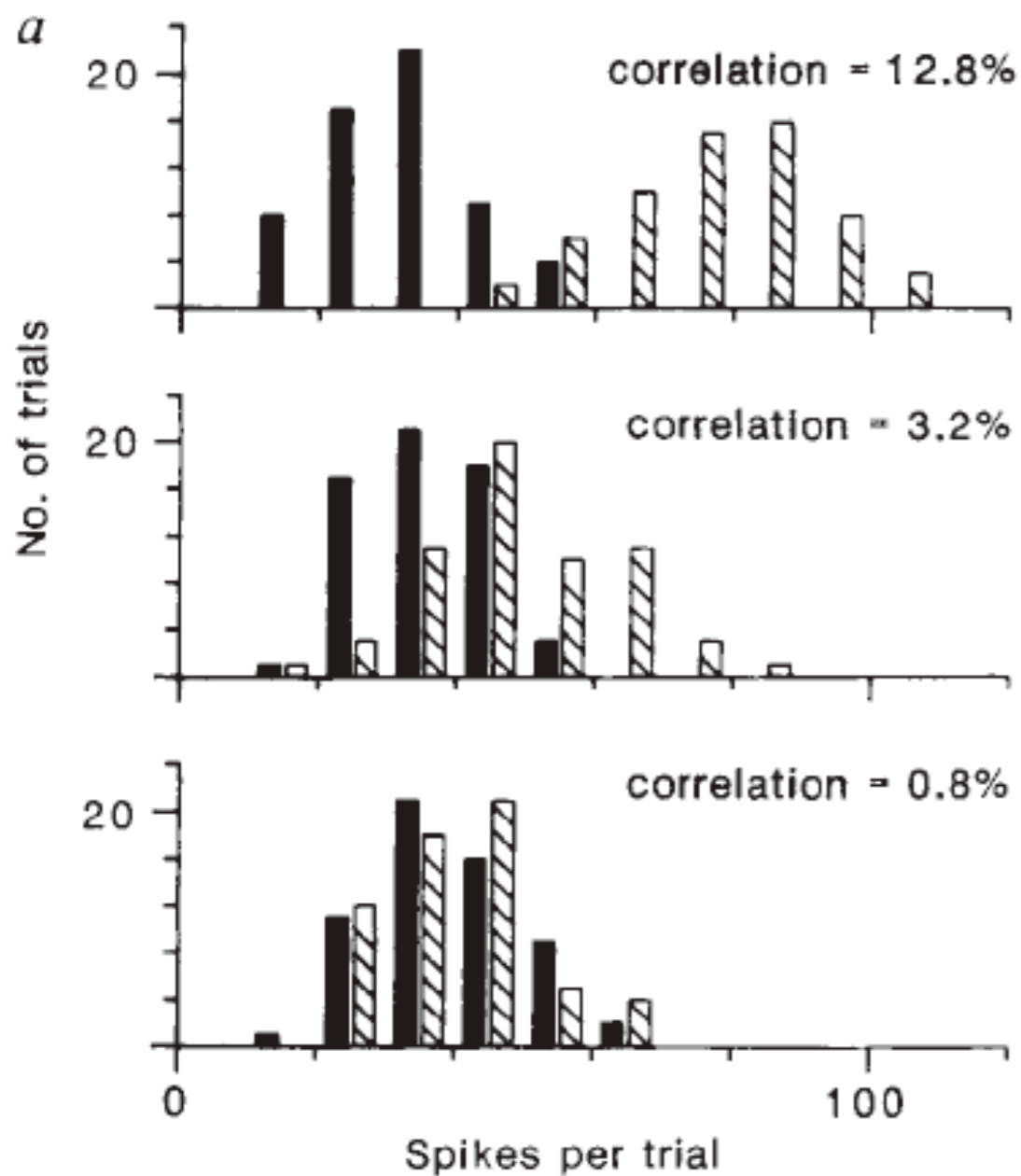
[W Schultz, P Dayan, PR Montague](#)  
[A neural substrate of prediction and reward](#)

# Neuronal correlates of a perceptual decision

William T. Newsome\*†, Kenneth H. Britten\*†  
& J. Anthony Movshon‡

\* Department of Neurobiology and Behavior, State University of New York,  
Stony Brook, New York 11794, USA

‡ Department of Psychology and Center for Neural Science,  
New York University, New York 10003, USA

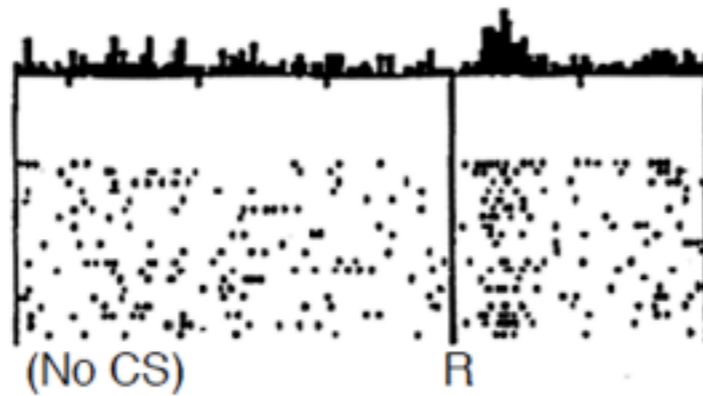


# A Neural Substrate of Prediction and Reward

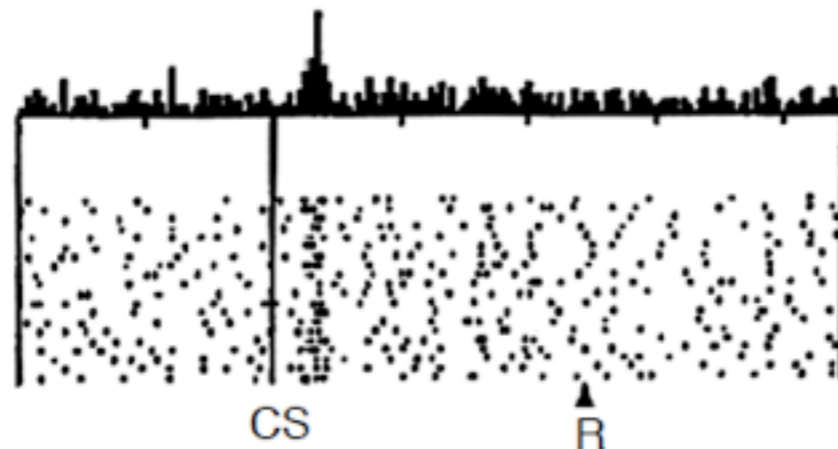
Wolfram Schultz, Peter Dayan, P. Read Montague\*

Do dopamine neurons report an error in the prediction of reward?

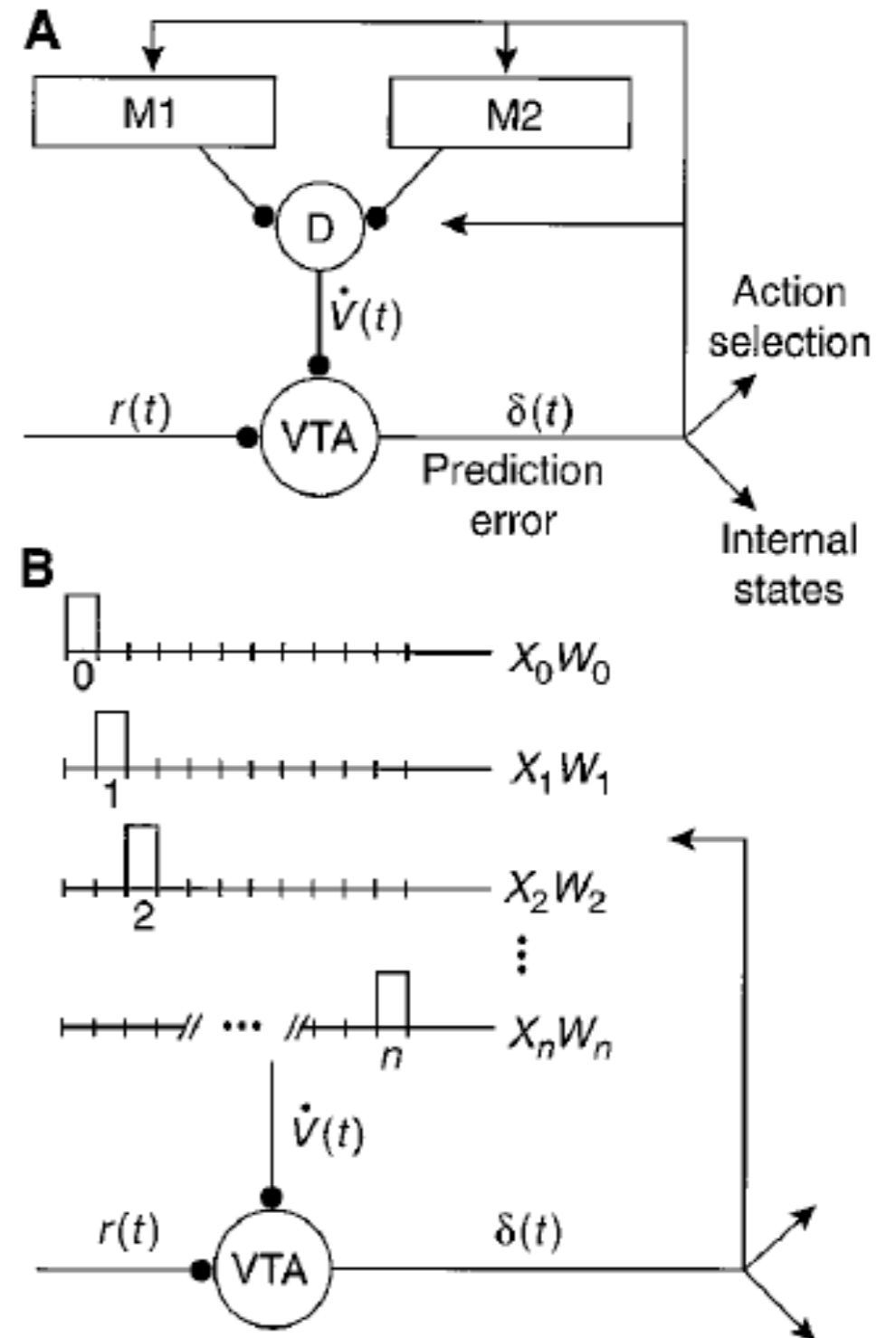
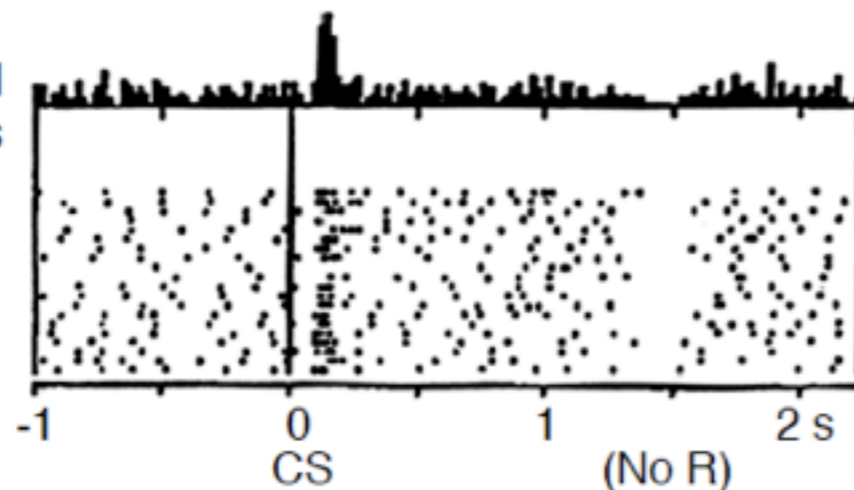
No prediction  
Reward occurs



Reward predicted  
Reward occurs



Reward predicted  
No reward occurs



# The Quest for the Neural Code

---

## Neuronal correlates of a perceptual decision

**William T. Newsome\*†, Kenneth H. Britten\*†  
& J. Anthony Movshon‡**

\* Department of Neurobiology and Behavior, State University of New York,  
Stony Brook, New York 11794, USA

‡ Department of Psychology and Center for Neural Science,  
New York University, New York 10003, USA

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## how is information represented in the brain?

Maybe it's the timing of spikes, rather than their average count (firing rate) that actually carries the information!

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**how much information does the population contain?**

Population codes are complicated because you cannot just add the information from different neurons if these are correlated (if they carry redundant information)



# The Quest for the Neural Code

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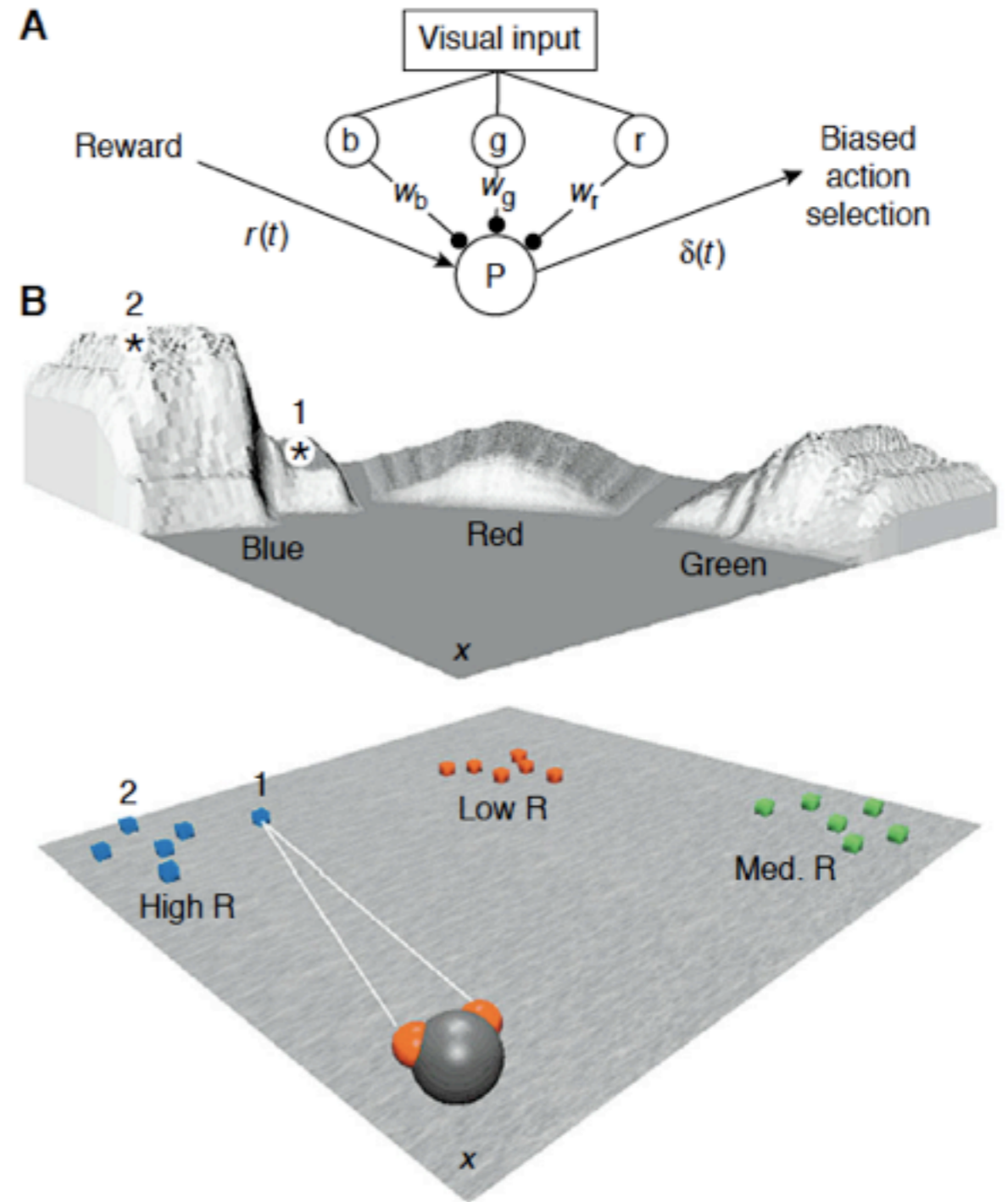
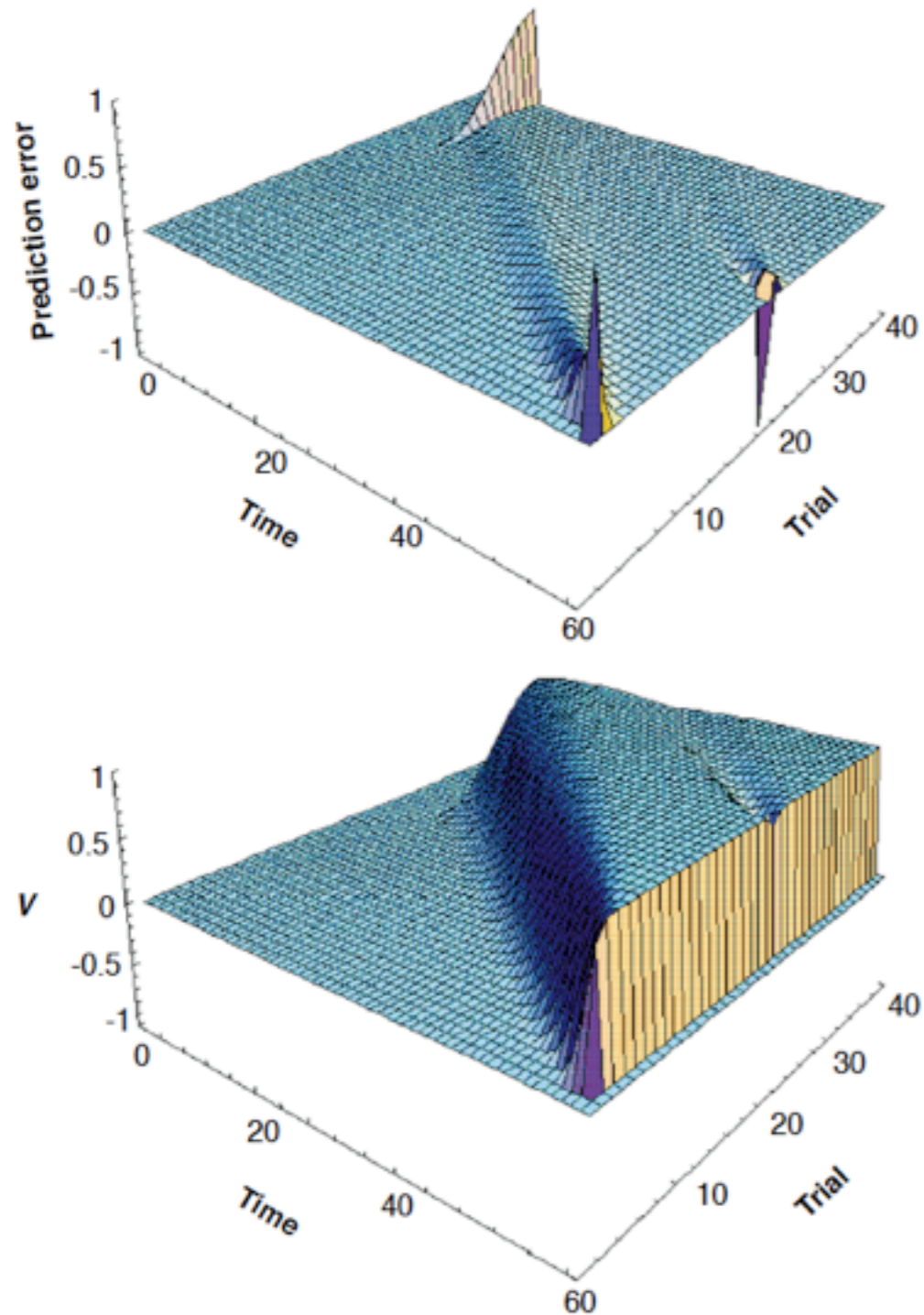
Population codes are complicated because you cannot just add the information from different neurons if these are correlated (if they carry redundant information)

## on what time scales is information represented?

In the article, stimuli are 2 sec long! But monkeys (and humans) integrate motion over much shorter time scales (100s of millisec) - then each neuron contributes less info!

# A Neural Substrate of Prediction and Reward

Wolfram Schultz, Peter Dayan, P. Read Montague\*



# How behaviors are learned

**A Neural Substrate of  
Prediction and Reward**

Wolfram Schultz, Peter Dayan, P. Read Montague\*



Edward Thorndike  
(1874-1949)

Psychology of  
Animal Learning

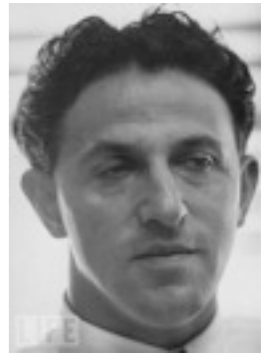
# How behaviors are learned



Edward Thorndike  
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Psychology of  
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Optimal Control  
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Richard Bellman  
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Marvin Minsky  
(1927-???)



Harry Klopf  
(1927-???)

Artificial Intelligence  
(Machine Learning)



# How behaviors are learned



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Theory



Richard Bellman  
(1920-1984)

Reinforcement  
Learning



Richard Sutton  
(1956-???)



Andrew Barto  
(1948-???)



Marvin Minsky  
(1927-???)



Harry Klopf  
(1927-???)

Artificial Intelligence  
(Machine Learning)